THE ASSOCIATION FOR COMPUTATIONAL HERESY

PRESENTS

A Record of the Proceedings of

# SIGBOVIK 2015

The ninth annual intercalary robot dance party in celebration of workshop on symposium about  $2^6$ th birthdays: in particular, that of Harry Q. Bovik

Carnegie Mellon University Pittsburgh, PA April 1, 2015



SIGBOVIK

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You hold in your hand the proceedings for SIGBOVIK 2015. Or, more likely, you're looking at them on a screen because you're too cheap to actually buy the proceedings. Either way, we thank you for your interest, but we thank you considerably more if you've demonstrated your interest by giving us money. As is traditional, we begin the proceedings with a message that nobody will read, but which must nonetheless be included because we don't want to give any of our authors the satisfaction of having their paper start on page 1.

We are proud to announce that SIGBOVIK has experienced a surge in interest in recent years. As can be seen in Figure 1, the number of submissions grew exponentially<sup>1</sup> from 2012 to 2014. We don't consider the number of submissions for 2015 here, because this message comes at the beginning of the proceedings and we wouldn't want to spoil the surprise. More people have been giving presentations, and attendance has been thriving. Of course, we don't keep numeric records of these facts, because that requires organizing, and does the SIGBOVIK organizing committee look like some group of people who are interested in organizing things?



Figure 1:  $y = 2 \times 10^{36} e^{-0.04x}$ , where y is the number of submissions and x is the year. Yeah, this graph was made in Excel. So what?

<sup>&</sup>lt;sup>1</sup>Exponential decay is just exponential growth with a negative exponent, right?

Because of these vast leaps in size, SIGBOVIK has reached that point in every young conference's life where we must consider splitting the talks into tracks to save time. Because time is money and all that. However, we at SIGBOVIK feel strongly that all attendees should be able to experience the full range of exciting research that SIGBOVIK has to offer, and so it is with great pleasure that we announce several proposals for creating two parallel tracks.

**Two concurrent presentations.** Two presenters stand at opposite sides of the front of the room and give talks concurrently. Audience members can sit closer to whichever presenter interests them more. For example, an audience member could give 25% of his or her attention to Presenter A and 75% to Presenter B by sitting one-quarter of the way to Presenter A's side of the room. Both presenters will display their slides, because the auditorium conveniently has two screens at the front of the room. We're not sure if they can show video from two different laptops, but this seems like a technical detail.

**Two concurrent presentations - in 3D!** As above, two presenters stand at opposite sides of the front of the room and give talks concurrently. However, we leverage advanced 3D technology to ensure that all audience members can fully appreciate both talks. Each audience member is given a pair of colored 3D glasses. One presenter wears red. One presenter wears blue. Their slides are colored accordingly and overlayed on one screen. The audience members' brains will correctly interleave the two presentations to form a coherent narrative. If the two presentations are in different fields, this probably opens us up to all kinds of funding for interdisciplinary research. We should look into that.

**Timeslicing.** Did you know that before your desktop had eight cores, it had only one, but you could still run multiple programs? This was accomplished through *timeslicing*. In the same way, two presenters can give talks concurrently by alternating slides. If this granularity is too high to achieve reasonable latency, the presenters could try alternating sentences, words, syllables or phonemes. The possibilities are endless.

**Question-and-answer optimization.** Frequent attendees of academic talks will notice that presenters spend approximately half of their total time answering questions, either during the designated question-and-answer period at the end of the talk, or when interrupted during the talk. A further observation is that attendees of talks are generally interested in asking questions or listening to the talk, but not both. We take advantage of these observations by having Presenter A give a talk and then answer questions, as usual, and Presenter B answer questions first and then give the talk. This may seem strange, but is really no different than normal because questions typically have little or no relation to what was discussed in the talk. This format has the benefit that those who wish only to ask questions can spend the entire session doing so, and those who wish only to hear talks can spend the entire session doing so. Additionally, both presenters are able to give their talks uninterrupted because anyone who would interrupt with questions is busy asking questions of the other presenter.

Of course, there is no reason to limit ourselves to two tracks, but the above solutions clearly generalize to *n*-track conferences, in the standard way. We hope to roll out one or more of these exciting developments for SIGBOVIK 2016 (not SIGBOVIK 2015, because we're lazy like that). And, with that, onto the proceedings!

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## Track X

# Locally Sourced, Lovingly Handresearched

## 1. inDRM: Copy Control with a Personal Touch

Miguel Lechon Keywords: DRM, independent game distribution, soft cryptography

### 2. A Hand-Held Device for User-in-the-loop Prin-ting James McCann and Notreal Author Keywords: users, loops, printing, users in loops, prin-ting

- 3. Artisanal Type Theory Carlo Angiuli Keywords: type theory, artisans, human computation
- 4. A Constructive Solution to the Koenigs-Pittsburgh Bridge Problem Greg. Hanneman and Benj. Blum

Keywords: KBP, KPBP, pittsbvrgh, sovth side, in order to honey themselves, thanks google translate

## inDRM: copy control with a personal touch

Miguel Á. Lechón<sup>\*</sup>

April 1, 2015

1

You say "I'll just make a copy for me and a friend", but he'll make one and she'll make one and when will it end?

> DON'T COPY THAT FLOPPY MC DOUBLE DEF DP[1]

## Abstract

inDRM is a digital rights management scheme. The goal of inDRM is ensuring that a small amount of human reflection accompanies the process of creating and distributing each new copy of a given piece of software. It is particularly well suited for developers that expect lots of passion but little money from their users, such as independent game developers.

Noteworthy properties of inDRM are its:

- Broken by Design design.
- P2P activation key generation.
- Distribution history record keeping.

Reference implementations and usage examples are available here<sup>1</sup>.

#### Motivation

#### 1.1 A brief history lesson

Home taping killed music thirty years ago due to music being distributed as passive, readily cloneable data. Too little was done to remedy this, and too late[2]. Computer software, in contrast, and by its own nature, needs to be active to fulfill its intended purpose, so, through the use of DRM, video games can choose to be as passive[3], aggressive[4] or passive-aggressive[5] as they so desire. This is the main reason why we have games, but not music, today.

#### 1.2 Danger lies ahead

The current dominant threat to the computer game industry is not so much economical as it is ecological. Shastri, Morrison and White provide a concise explanation in their recent discussion[6]:

It's a total SNAFU! Adults buy all kinds of games but never play them. Kids have time to play but behave like monomaniacs... *Minecraft* this or *LoL* that, day in, day out!

<sup>\*</sup>e-mail: miguel.lechon+inDRM@gmail.com <sup>1</sup>https://github.com/debiatan/inDRM

Soon we will all realize there are no *gamers* left. And when the bubble bursts, the reeking corpses of unplayed *Steam* libraries will wash this industry away.

Indeed, according to undisclosed sources at *Valve*, the average library *backlog* (bought but unplayed games) amounts to 83% of the total number of titles each user owns[7].

#### 1.3 Danger knocks at the door

The vast majority of game developers do not see financial return as an end, but as a way of measuring the engagement of players to their games. However, in today's prosperous economical climate, money is essentially thrown at the feet of game developers for no apparent reason, tricking them into thinking they are succeeding when, in all likelihood, no one is playing their creations.

A recent example is the case of the *Hand-made Hero* project[8], where one programmer with no previous history of ever completing a commercial video game announced his plans of working five hours *per week* on a yet-to-be-started title. He successfully collected thousands of preorders during the course of the following weeks.

Will this summer last much longer? Won't some brilliant academic mind devise a clever way of avoiding this impending disaster? How can cautious game developers gauge the *real* commitment of their user base when all signs indicate they are doing a splendid job?

The answers to these questions are *no*, *yes* and *read on*.

#### 1.4 Fear no more

The solution, of course, lies in the repurposing of the industry's proven old savior, DRM.

As long as money keeps growing on the trees of developer's backyards, the amount of game copies sold will be an inaccurate measure of consumer acceptance. Instead, I propose making players spend an ultimately much more valuable resource than money: their time. In order to achieve this, and as a condition to unlock the game, the user will be forced to engage in a short social exchange with either the creator of the game or some other fellow player.

By slightly inconveniencing potential clients, creators can expect to gain a clearer understanding of the appeal of their games and end up with a much more committed, albeit smaller, user base.

## 2 Cryptological interlude

inDRM's strength rests on:

- the solid foundation of the MD5/4 cryptographic hash function
- the RSA public key cryptosystem signing procedure [10] with a key length of 32 bits
- the identification of computers via the MAC addresses of their primary network interfaces.

This section consists of a rather in-depth review of the first two algorithms.

#### 2.1 MD5/4

MD5[9] takes an arbitrary string of characters, passes it through a deterministic blender and produces an unnecessarily long 128-bit value.

MD5/4 takes that value, chops it into four 32-bit pieces and XORs them together to produce a more digestible 32-bit digest.

#### 2.2 RSA signatures

The RSA signature procedure is a popular party trick from the late 1970s, where one person comes up with three numbers n, d and e that satisfy the following property:

 $(x^d)^e \equiv x \pmod{n}, \forall x \in \mathbb{Z}^{-2}$ 

That person then makes **n** and **e** public, spends a few minutes teaching modular exponentiation to the crowd and claims to possess the ability to:

- Turn any message into a number **x** (using a scheme similar to MD5/4)
- Produce a number y that depends on x and that acts as that person's signature of the message, fact which can be verified by checking that:  $y^e \equiv x \pmod{n}$

Of course, behind the scenes, the entertainer obtains y by raising x to the dth power, dividing the result by n and taking y to be the remainder of that division.

The process of finding the three initial numbers is demonstrated in [11] and can be

easily accomplished today with the help from the time-tested software package openssl[12] by issuing the following command in any POSIX-compliant operating system:

openssl genrsa 32|openssl rsa -text<sup>3</sup>

Looking at its output, the modulus field is equivalent to our n, publicExponent denotes e and privateExponent indicates d.

## 3 Guided tour

Any person in possession of an unlocked instance of a game protected by inDRM can unlock copies for other potential players, as long as those copies descend, directly or indirectly, from that same unlocked instance.

There are several distinct phases in the distribution of a game protected by inDRM:

- Author **A** of a game generates a *root activation key file* and distributes it along with the game
- Potential player **P** obtains the game, tries to run it and is invited by the software to generate a *request file* and send it back to author **A** as a precondition for playing
- Author A receives the *request file*, throws a small party and generates a *response file* for player P that becomes a valid *activation key file*
- Player P plays the game, finds it worthwhile and hands a copy to friend F

<sup>&</sup>lt;sup>2</sup> Which translates into Pythonist parlance as: (pow(pow(x,d,n),e,n) == x) == True for any integer value of x

 $<sup>^{3}</sup>$ It is fashionable to use 2048 instead of 32, probably in reference to the homonymous video game[13]

- Friend **F** tries to run the game and is invited by the software to generate a *request file* and send it back to either **A** or **P** as a precondition for playing. **F** chooses to contact **P**
- P generates a *response file* for friend F, by virtue of possessing a valid *activation key file* belonging to the same *key chain* that reached F

• ...

The rest of this section reviews the technical details behind the generation of key files.

#### 3.1 Root activation key file

The creator of the game generates a root activation key file and distributes it with every copy of the game. In and of itself, that key file only allows the game to be played on the developer's computer. However, it provides the basis for the generation of key requests from potential players.

Here is an example of an inDRM root activation key file:

\_ hash: c738b172

signature: d38cc9a

Inside key files, lines starting with an equal sign are ignored. The rest are composed of a tag, followed by a semicolon and a value field. The tags and their associated functions are these:

game: Title of the game

nick: Author's name or nickname

location: Author's place of residence

**date**: Date of creation of the key file (in *yyyy/mm/dd* format)

notes: Notes from the author

mac\_salt: Random 32-bit hex number

mac\_hash: MD5/4 hash of the concatenation of mac\_salt and the hexadecimal representation of the MAC address of the primary network interface of the computer generating the key file

hash: MD5/4 hash of the concatenation of: the preceding **signature** in the key chain (assumed to be "0" in case of the master key file), game, nick, location, date, notes, mac\_salt and mac\_hash

**signature**: RSA signature of **hash** (computed as (hash<sup>d</sup> mod n), where d and n have been generated along with e as discussed in section 2.2).

For the particular example used in this section, the values of the cryptographic parameters are:

- n (modulus): 3333098473
- e (public exponent): 65537
- d (private exponent): 939472245

These values are to be embedded in the inDRM routines present in the game. The pair (e, n) will be used as an RSA public key in order to check signatures present inside key files. The pair (d, n) will allow a registered copy of the game to sign key file requests from new potential players through an in-game menu option labeled to that effect.

# 3.2 Activation key file validation

Every time a piece of software guarded by inDRM is run it reads the activation key file and checks that:

- the value of the **hash** field is correct (by recomputing it using the tag values that precede it)
- the value of the **signature** field is correct (by ensuring that **signature**<sup>e</sup> mod  $n = \mathbf{hash}$ )

If these two conditions are met, the primary MAC address of the machine is checked to see if it satisfies:

 $\frac{\text{MD5}}{4}(\texttt{mac\_salt}_i + \text{MAC}) = \texttt{mac\_hash}_i$ 

(where the '+' sign indicates concatenation of strings) for any mac\_salt<sub>i</sub>/mac\_hash<sub>i</sub> pair present in the file. If it does, the game is allowed to run. Otherwise, the user is invited to generate a request file.

#### 3.3 Request file generation

An invitation to generate a request file will essentially convey a message similar to this one: \*\*\* Last MAC address on key file does

not belong to this computer \*\*\* You won't be able to play this game unless you convince another player to generate a key for you.

Let's build a request file...

Please provide the following data
(or press 'enter' to skip):
Name (or nickname): \_
Location (place of residence): \_
Notes (message to future players): \_

After providing (or failing to provide) the three pieces of information, inDRM collects the date and MAC address of the system, generates the request file and tells the user that:

A request file has been generated here: \*\*\* /home/ ... /request.txt \*\*\*

In order to finish the registration process, send that file back to whoever shared the game with you. That person will be able to unlock your copy.

Think twice before sharing this game with other people. If they ever try playing it, they might come back asking you to register their copies.

The request file consists of a copy of the original key file distributed with the game with an extra section appended at the end. Imagining that the original key was the one presented back in section 3.1 and the user provided "miguel", "barcelona" and "this

sucks" as values for **name**, **location** and **notes**, respectively, the resulting extra section could look like:

```
nick: miguel
location: barcelona
date: 2015/04/01
notes: this sucks
mac_salt: 95be1f47
mac_hash: 6051a20a
hash: 1f495ce2
signature: NO SIGNATURE YET
```

In order to run the game, the potential player will then send the request file up the distribution chain for it to be signed.

#### 3.4 Response file generation

The example activation chain we have described consists of only the original author of the software and its first user. The request file will then be necessarily sent to the author, who will execute a registered copy of the game and select the option that allows to sign requests. That routine will check that:

- the values of all **hash** fields are correct (by recomputing them using the values of fields preceding it)
- the values of all signature fields, except for the last one, are correct (by ensuring that (signature<sup>e</sup> mod n = hash))
- the primary MAC address of the computer satisfies:

 $\frac{\text{MD5}}{4}(\texttt{mac\_salt}_i + \text{MAC}) = \texttt{mac\_hash}_i$ for some <code>mac\_salt\_i/mac\_hash\_i</code> pair in the request file.

If all three conditions are met, the last **signature** field of the request file will be completed with the help of the private exponent **d** and the modulus **n**:

```
signature = hash^d \mod n
```

In our example, this would mean modifying the last **signature** of the request file to read:

#### signature: 9bc727d0

The resulting file will then be sent back to the potential player to be used in place of the original activation key file. The *potential player* will then stop being just *potential* and start a new life as a *real player*.

## 4 **Properties**

Improving security typically means degrading usability. Providentially, both effects are intended consequences of the use of inDRM.

There are several other desired properties that have gone into the design of the inDRM copy control scheme. This section discusses them briefly.

#### 4.1 Broken by Design design

If we were to depict the concept of security as a one-dimensional horizontal segment delimited on the left by the word *insecure* and on the right by the word *secure*, *inDRM* would lie definitely to the left, in a place probably labeled as *cryptographically annoying*. Sadly, space limitations preclude even a cursory exploration of all the security flaws exhibited by *inDRM*.

#### 4.2 P2P key generation

Players of games protected by inDRM can rest assured that they will be able to enjoy them for as long as they are interested in doing so. The absence of network authentication and the distributed nature of the key generation process guarantee that.

Moreover, as a side benefit of the distributed nature of the key generation scheme, players might derive some sense of belonging to a community by simple inspection of the contents of their personal key files. Intensely imaginative players, of the kind that take pleasure in trading *Steam* inventory items, may even experience inDRM's compulsory chaining of signatures as a tradition that makes them part of a lineage.

# 4.3 Lack of attractive as a cracking target

All DRM schemes are eventually subverted, so one should not ask *if* but *when* will **inDRM** be broken. I suspect that it will not happen any time soon for mainly two reasons:

- Breaking inDRM poses no challenge, so no one can take pride on that endeavor
- The only benefit to be derived from breaking inDRM is the avoidance of a short social interaction

# 4.4 Distribution history record keeping

Key files have potential uses other than game distribution control. For instance, the com-

bined **notes** sections of a key can be used as a simple guestbook or, perish the thought, a space for advertisements.

Another more elaborate use requires us to picture the set of activation key files associated to a particular game as a tree, its *leaf* key files being the ones that carry the most information. Getting hold of a sizeable percentage of those files by some means<sup>4</sup>, would facilitate the identification of the principal hubs in the game's distribution network.

## 4.5 Simplicity

MD5 is straightforward to program[14]. The improvements that MD5/4 introduces come at the cost of three extra XOR instructions.

Implementing the standard RSA algorithm would require working with arbitrarily long integers, but the 32-bit version of it does not impose that hardship on game developers. Two additional benefits of working only with 32-bit values are that key files become smaller in size and that they fit inside the two-column layout of this article.

#### 4.6 Involvement of players

In order to acquire a valid activation key file, the potential player must secure the collaboration of another player. After implicating that other person, the new player may feel pressured to give the game a proper try and avoid dropping it after just a few minutes of play.

<sup>&</sup>lt;sup>4</sup>such as asking nicely or offering players extra game content in exchange for their keys

#### 4.7 Future-proof architecture

As long as one registered copy of the game remains, it will continue to be redistributable and playable. Even if no registered copy remains and even if the game binary proves difficult to crack, bruteforcing the **signature** of a request file requires just the testing of the set of  $2^{32}$  possible signatures.

## 5 Conclusion and final remarks

Game developers do not need protection from software pirates; they need instead to be guarded from the uncaring capricious moneythrowing player hordes that endanger their profession. By choosing to distribute games guarded by inDRM, they are not only deciding to acquire a much more mature following, but are also telling the video game community that *they care*.

For an up-to-date list of games that use inDRM, check:

http://blog.debiatan.net/inDRM.html

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Pseudocode
```

<sup>&</sup>lt;sup>5</sup>https://www.youtube.com/watch?v= up863eQKGUI

<sup>&</sup>lt;sup>6</sup>https://en.wikipedia.org/wiki/Sony\_BMG\_ copy\_protection\_rootkit\_scandal



Paper 1: inDRM: copy control with a personal touch

Chris Martens Rating: 2 (destroy all games) Confidence: 4/4

The copy protection scheme described in this paper ostensibly poses a solution to a threat to the video games industry. As such, I cannot sanction it as a good idea. Also, the paper is eight pages long and had a lot of boring stuff about crypto in it.

On the plus side, the "Broken by Design" design seems like a useful feature.

## A Hand-Held Device for User-in-the-loop Prin-ting

James McCann\* TCHOW Notreal Author WeAreWe University



**Figure 1:** Our handheld hardcopy output device (left) shares many of the capabilities of a commerially produced printer (right), but in a much more convenient form-factor.

#### Abstract

Thanks to the proliferation of the ARPANET, computers are used every day by hundreds of people around the world to access a wealth of information. However, until recently, this information could only be applied in domains that could be brought within reach of a computer terminal, or by operators with extensive memory training.

With the advent of the *printer*, this has begun to change. Computer operators now are able to send digital information to a machine which converts it into *hardcopy*, a physical representation constructed from marks on paper. This hardcopy information can then be transported to application locations distant from any computer access terminal and applied.

While this process is certainly more user-friendly than the alternatives of relying on memory or movement of information application domains, it remains cumbersome, expensive, and inaccessible. We propose a hand-held device which can produce informational markings on paper, much like a printer. Hardcopy produced with our device has similar information content to that produced with a conventional printer, but at a lower price.

Further, we describe *user-in-the-loop printing*, a process enabled by our device, which allows computer operators to filter and transform information as it flows from the computer to the hardcopy. These transformations can lead to ink savings through domain-tailoring. We also demonstrate how our device can allow computer operators to increase the information output of existing hardcopy – either from a conventional

printer or our own device – through a process we term *information overlay*.

CR Categories: B.5.2.s [Rock]: Rock—Lobster

#### 1 Introduction

ARPANET [Davies et al. 1967] is an inter-network of computers, which are able to exchange information between themselves using digital network signalling. Estimates vary, but most experts [Callahan and Hodgman 1971] agree that between tens and hundreds of people use the ARPANET every week, transmitting – in aggregate – more than 400 *kilobytes*<sup>\*</sup> of data during the average month.

However, until recently [2014], this information was confined to locations with direct ARPANET access, such as "ARPANET Cafes," or to those locations to which computer operators with exceptional memory skills could travel, such as "Cafes." However, with the advent of *printers*, this restriction has been relaxed.

In this paper, we extend the notion of *printing* with a handheld hardcopy output device. Our device provides many of the same output capabilities of a full-scale *printer*, without requiring a movable type department or access to steam power (a significant cost savings). Further, our handheld device enables *user-in-the-loop prin-ting*, through which the computer operator can actually transform the information which they record.

<sup>\*</sup>e-mail: ix@tchow.com

<sup>\*</sup>A *kilobyte* is unit of information equal to the storage capacity of 64 *kilograms* of quarters (practitioners often summarize this by saying there are "sixteen bits in one byte".)



Figure 2: A labeled diagram of our hardcopy output device. For more information see the text.

### 2 Our Tool

A prototype of our hardcopy output device is shown in Figure 1, with a schematic diagram shown in Figure 2. We briefly explain the construction here. Curious readers are invited to submit an NDA request to the second author to be granted access to further details.

The operative end of the device is the *rolling tip*, which distributes ink from the *fluid reservoir*. In non-printing situations, the rolling tip is protected by the *tip cover*, which is also is the anchor point for the *adjustable fin* – which we believe contributes to the overall aerodynamics of the device.

The fluid resevoir is surrounded by the *cylinder hand interface*, which – as the name suggests – is the control surface through which the device is actuated during printing operations.

Finally, the *neck strap* is an ergonomic addition aimed at mitigating hand fatigue during long printing sessions.

## 3 Basic Operation

During a basic printing session, the operator first secures the neck strap to the device and adjusts it for optimal comfort. The operator then transfers the tip cover from the rolling tip end of the device to the tip cover storage location on the non-tip end of the cylinder hand interface. Next, the operator secures a piece of printing substrate to their video ARPANET computer terminal device, and – controlling the rolling tip's position with the cylinder hand interface – directs our device to move along the printing substrate in the patterns visible through it.

This has the effect of creating ink deposits on the substrate, registered to the ARPANET information the operator wishes to capture.

Though this process may sound complicated, we find that most operators become proficient withing the first 1-2 weeks of incarceration in our specialized training camp, at which point they are allowed to return home.



**Figure 3:** User-in-the-loop prin-ting allows users to excerpt just the information they require from a document (sinister), unlike conventional printing, which reproduces the entire text (dexter).

#### 4 User-In-The-Loop Prin-ting

Our hardcopy output has many advantages over a commercial printer. One large advantage is that – because the user is controlling the device – they are able to transform the information that is recorded. We call this process *user-in-the-loop prin-ting*.

In this section, we summarize the *prin-ting* actions taken by a group of computer operators using our device. We recruited these operators through an ARPANET posting, and in no way threatened or cajoled them into participating. We list only the most common operations, since we think that a more detailed list is probably worth saving for a second publication.

#### 4.1 Condensation

One of the most common transformations we observed was the removal of extraneous textual information. This information removal allowed users to speed up their hardcopy production process by omitting all but the most pertinent details.

Often this would involve the elimination of entire paragraphs and sections, save for a few key equations or phrases. This is a huge material and time savings that cannot be accomplished by commercial printers.

#### 4.2 Abstraction

Abstraction is the graphical analogue of condensation. Often, when tasked with producing hardcopy of a particular image, operators would remove much of the detail from the image; reproducing an approximation with only a few strokes.

As with condensation, we found that the level of detail reproduced was often task-dependent. For instance, when producing hardcopy of a map, users were likely to carefully reproduce streets near their intended journey or destination, and simplify or elide streets elsewhere.

#### 4.3 Spelling Alteration

During the course of hardcopy production, we often saw users change the spelling of words. We believe that this is a positive indication that our handheld printing device can contribute to the evolution of our living language.

#### 4.4 Incremental Refinement

Finally, several of our participants used an unexpected, but exceedingly efficient, printing strategy, wherein a document produced on a traditional printer was refined using our hardcopy output device.

Though this hybrid output scenario was unexpected, we found that its unexpected unexpectedness was not something we expected, but we would not expect that follow-up work in this unexpected direction would be unfruitful. So such follow-on work shouldn't be unexpected, unlike this unexpected behavior, which wasn't something that was not unexpected.

#### 5 Limitations

Our handheld printing device does have a few limitations, as compared to a traditional printer. But none worth mentioning.

#### 6 Conclusion

In this paper, we described a revolutionary device that enables computer operators to produce hardcopy without the need for an expensive printer. In testing, we observed that operators used our device not just to produce exact copies of documents, but actually significantly transformed those copes (p < 2.0). We termed these transformations *user-inthe-loop prin-ting*. We have only tested our hand-held printing device on flat surfaces; however, we are excited about the possibility of recording information on non-flat surfaces – a process we term "3D printing". We believe *user-in-the-loop 3D printing* has the potential to revolutionize the decorative arts.

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#### A Even Prime Numbers

$$p_{\text{even}} = \{2\}\tag{1}$$

#### **B** Integral Roots of Unity

$$\{n \mid n \in \mathbb{Z}, n^2 = 1\} = \{-1, 1\}$$
(2)

#### C Composite Prime Numbers

Ø

## Artisanal type theory

#### Carlo Angiuli

April 1, 2015

#### 1 A brief history of some things

Food was invented by Mesopotamians some 5,000 years ago, and has been eaten ever since. Logic was invented in the Mediterranean by ancient Greeks, including Aristotle and a mortal man [1] named Socrates. It lives on as an important course in pre-law curricula across the United States.

Modern times require more modern logics. Computer programming is closely tied to *intuitionistic* logic, in which proofs of a proposition correspond directly to algorithms. Intuitionistic logic, often in the form of type theory, is taught to several American computer scientists annually.

Until the past several centuries, food and logic were primarily manufactured by artisans, who trained apprentices in the arts of, respectively, proofing and proving. The Industrial Revolution gave rise to machines able to produce food and textiles much faster than artisans ever could. The digital revolution, likewise, has turned 'computer' from a human job into a cheap, ubiquitous machine capable of multiple calculations per second.

Despite the overwhelming success of mass-produced food, some consumers want to revisit food's roots as a product sustainably and ethically crafted by local artisans using traditional techniques. The result, known as *artisanal food*, has taken off in popularity in the past few years [2, 4].

#### 2 Algorithms with the human touch

So too should computer scientists return to the roots of computation—slow, error-prone calculations performed by humans. After all, despite the close relationship between computer programs and type theory [3], or indeed, between computer programs and algorithms, there is no need to involve computers in deeply human tasks like sorting lists, routing packets, or decoding MPEG-4 video streams.

We advocate a more personal approach to computation, called *artisanal type theory*. Artisanal type theory has the same rules as ordinary type theory, except that all terms and typing derivations must be handwritten. Closed, well-typed terms evaluate to values of the same type, accompanied by a certificate of authenticity that a human performed that evaluation.

Since each term was lovingly handcrafted and normalized, these artisanallyperformed beta-reductions provide a more *meaningful* explanation of type theory than traditional computer-based interpreters. Using artisanal type theory demonstrates a firm commitment to *locally*-grown, sound, and complete reasoning systems.

#### 3 Examples

**Shallow learning.** We can implement artificial intelligence using human intelligence. Given the training data that **false** is desired but **true** is not, one can manually build a classifier for booleans. Such a classifier can then be run on a boolean to determine whether or not it is in the desired set. In the example below, we run the classifier on **false**.

x:bool + x:bool x:bool + false : bool x:bool + true: boo x:bool + if x then false else true : bool	Γ
· + Xx: bool. if x then false else true: bool → bool	· + false : bool
· ~ ( ) X: bool. if X then false eke true) false	e : bool
≡ [false/x](if x then false else true) ≡ if false then fake else true ≡ true	Lovingly Reduced by Carlo Angiuli 3/16/2015

Fairly quick sorting. Artisanal computation has some advantages over computer programming—namely, humans can perform some computations without needing a precise algorithm. In this example, we sort a list of integers without the need to specify a particular sorting algorithm.

I can do that	trivial?		
<ul> <li>F Sort : int list → int list</li> </ul>	·+ [3,7,9,-1,4] : int list		
• + sort [3,7,9,-1,4	]: int list		
≅ [−1,3,4,7,9]	LOCALLY EVALUATED IN PITTSBURGH 3/16/2015		

**Small-batch jobs.** We can also write scripts which artisanally perform repetitive computing tasks such as renaming a large number of files, accessing sequential URLs, etc. Doing so requires adding primitives for I/O, file system access, and so forth. As discussed above, it is unnecessary to actually implement these primitives, because the human runtime already supports these tasks via a computer's traditional user interface. Furthermore, unlike in traditional scripting languages, it is easy to extend this with physical-world primitives such as eatLunch, writeHandwrittenThankYouNote, and sleep.

#### 4 Conclusion

We hope artisanal type theory will appeal to computer scientists and mathematicians who appreciate algorithms but believe computers themselves are quite inconvenient at times. Unlike ordinary type theory, it directly expresses computations as if people, but not computers, matter. Therefore, we are hopeful that artisanal type theory will be a useful foundation for the field of *human science*.

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## A CONSTRUCTIVE SOLVTION TO THE KÖNIGS-PITTSBURGH BRIDGE PROBLEM

Greg. HANNEMAN Language Enthusiast and Errant Scribbler Carnegie Mellon Vniversity Benj. BLVM Light Cone Sedentarian Carnegie Mellon Vniversity

#### ABSTRACT.

We walked across a bunch of bridges one day.

#### §1..... BACKGROVND.

Figure 1 and Definition 1 state the well-studied Königsberg Bridge Problem [Eul41].

Definition 1. The Königsberg Bridge Problem (KBP).

Regiomonti in Borussia esse insulam A der Kneiphof dictam, fluviumque eam cingentem in duos dividi ramos, quemadmodum ex figura videre licet: ramos uero huius fluvii septem instructos esse pontibus, a, b, c, d, e, f, et g. Circa hos pontes iam ista proponebatur quaestio, num quis cursum ita instituere queat, ut per singulos pontes semel et non plus quam semel transeat.

According to the best modern scholarship, it is thought that this passage reads as follows.

"At Königsberg in Prussia there is an island A known as Kneiphof, and flowing around it is divided into two branches, as shown in the figure; and the branches of the river, seven bridges, however, of this, a, B, C, d, a, e, F, and G. Already presented to him, the question concerning these bridges is, the course to be instructed so to whether a person may be able to, and not more than once in order to pass one by one the bridges honey themselves."

The criteria expressed in Definition 1 have been generalized to arbitrary geographical



Figure 1: Kaliningrad, Russia (colloq.); better Known in the Formal Literature as Königsberg, Prussia

topologies. Of extreme local interest is the instance derived from the city of Pittsburgh, Pennsylvania, V.S.A., as Definition 2.

Definition 2. The Königs-Pittsburgh Bridge Problem (KPBP).

Cross every pedestrian-navigable trans-Three-River bridge with at least one endpoint in the city of Pittsburgh, exactly once, to be accomplished during one continuous circuit.

This article presents a constructive proof for the existence of a solution to KPBP. Furthermore, while most prior work [Wal15] has largely focused on theoretical analysis of KBP variants based on graph theory, here we additionally offer a more practical approach based on ambulation theory.

#### §2..... FORMALIZATION.

The formal statement of KBP inquires after the existence of an Eulerian path on a graph representing Königsberg, with one node to repre-



Figure 2: informal Diagram of the Topology of Pittsburgh, Pennsylvania as defined by its Bridges and Rivers.



Figure 3: Formalization of Figure 2.

sent each of the landmasses connected by various edges (bridges). In KPBP we simply change the graph to represent the topology of our home city (Figure 2). $^1$ 

Vnlike KBP, in KPBP we require an Eulerian circuit, rather than an Eulerian path. Recent developments in ambulation theory have shifted the common wisdom towards a preference for the use of circuits over paths in ambulatory proofs, as the circuit presents a more convenient practical application. (Put in more intuitive terms, the Eulerian circuit allows the bridge-walkers to sleep in their own beds the following night, rather than being stranded across a river.) Fortunately, the topology we have selected for KPBP allows for such a solution..

#### §3..... PROOF.

Theorem 1. The Königs-Pittsburgh Bridge Problem is solvable.

We present here a constructive solution to the problem, first given by Hanneman, Vangpat, and Blum (2012, Oct. 27, 5:15 a.m.-10:05 p.m.). The full solution has length 35 miles and consumes approximately 17 hours of wall-clock time. We depict R in two distinct styles, in a somewhat abbreviated form, in Table 1 and Figure 4.

Intermediate details may easily be filled in by following Procedure 1.

Procedure 1. Let R be the given solution route for KPBP, p be a position along it measured in miles from the start of R, and  $\hat{\mathbf{r}}_{\mathbf{x}}$  be a unit vector in the direction of R at position x.

$$\begin{array}{ll} \mbox{while } p < |\mathbf{R}| \mbox{ do} \\ \vec{d} \leftarrow \mbox{StepSize} \cdot \hat{r}_p \\ \mbox{Walk}(p, \vec{d}) \\ p \leftarrow p + ||\vec{d}|| \\ \mbox{end while} \end{array}$$

Remark 1. Some experimental determination will of course be necessary to arrive at the correct value of the StepSize variable. We suggest a default value of 75 cm, to be adjusted upwards or downwards as personal height and local terrain require.

Lemma 1. Walkability.

A point p' along R can be reached from point p along R, following Procedure 1, assuming p < p'.

 $\square$ 

e

Lemma 1 thus establishes a "modus ponens" result for traversal of the route R from its beginning (p = 0) to its end  $(p = |\mathbf{R}|)$ . This is, however,

Node	Edge	Node		Node	Edge	Node
EE	HP	NS	1	NS	FtD	EE
$\mathbf{NS}$	62	EE		EE	FtP	SS
EE	40	NS		SS	SF	EE
$\mathbf{NS}$	16	EE		EE	10	SS
EE	RaC	NS		SS	Lib	EE
NS	AW	EE		EE	BH	SS
EE	RoC	NS		SS	HMS	EE
NS	MKR	SS		EE	GF	SS
SS	WE	NS		SS	HSG	EE

Table 1:  $|\mathbf{R}| = 35$  mi.

<sup>&</sup>lt;sup>1</sup>The astute observer will note that no edge among our formalism represents the 32<sup>nd</sup> street bridge. During the progress of our research, this bridge did not exist due to construction, and hence is omitted. If added to the graph (call it KPBP'), it is known that a non-cyclic solution exists, but a constructive proof is left to future work.



Figure 4: a cartographic Rendering of the Solution Route R.

a purely theoretical result. We now show the practicability of the solution in an operational scenario via a number of satisfiable conditions.

Condition 1. Initialization.

Let A be a set of attempting participants. Then a must be present at p = 0 Va  $\in$  A.

Condition 2. Progression.

Let B be a set of qualifying bridges such that the following are true  $\forall b \in B$ : (1) b satisfies the bridge criteria from Definition 2; (2) b has defined  $0 \leq p_b \leq 35$  on R. Let  $b_i$  be the ith ordered element of B, and let |B| = n. Then  $C = \{c_1, ..., c_n\}$ , and  $c_i = (S_i, b_i)$  iff some  $S_i \subseteq A$  crosses  $b_i$ .

Condition 3. Termination.

Let the set of ending participants  $E \subseteq A = \{a \in A \mid a \in S_i \ \forall i\}$ . Then the solution is successful iff  $E \neq \emptyset$  and e is present at  $p = 35 \ \forall e \in E$ .

Lemma 2. Satisfiability of Conditions. Conditions 1–3 are satisfiable.

Proof. Set  $A = \{A | an, Ben, Dan, Greg, Keith\}$ . Note that  $Pr(x \text{ awake at 5 a.m.}) = \epsilon \ \forall x \in A$ . As long as  $\epsilon > 0$ ,  $\epsilon^5 > 0$ . [VII14]

Set B = {Highland Park, 61st Street, 40th Street, 16th Street, 9th Street, 7th Street, 6th Street, McKees Rocks, West End, Fort Duquesne, Fort Pitt, Smithfield Street, Liberty, 10th Street, Birmingham, Hot Metal, Glenwood, Homestead Grays}. The bridge criteria of Definition 2 are satisfied  $\forall b \in B$ . Therefore the set C of crossings may be freely constructed following R from Figure 4.

Finally, set  $E = \{Alan, Ben, Greg\}$ . The diagrams in Figure 5 offer a visualization of these values for A, B, and E.

Since  $|\mathbf{E}| = 3 > 0$ , this proves Lemma 2 and thus the successful instantiation of Conditions 1-3. Together with Lemma 1, this proves that R is a navigable Eulerian circuit of the city of Pittsburgh. Therefore a solution to the Königs-Pittsburgh Bridge Problem exists.

#### §4..... CONCLVSION.

Vetere Konigsberg consequat pons (KBP) designat insulae urbem, flumina, pontes, qui in tali figuratione transiens per singulos semel iter unum non potest. In hoc articulo quaestionis exposuimus accommodatio hodierna die ad oppidum Pittsburgh (KPBP). Significat adaptationem ad profectum nostrum insignis civitas-in-es super duobus.

Vno modo, sicut KPBP est solubilis, offert mathematici nostram collationem incitamentum ad ire foris, et accipiam ab eo aliquid exercitium, quod hodie magis quam somnium, quod fieri non potest. Deinde insuper offerebat speculativa ratio nos instruit etiam problema aedificant, qui probi ad ultimum pedes decem milia multa mala!

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(a) Condition 1, Initialization.



(b) an example Member of the set B.



(c)  $\mathfrak{A}\mathfrak{b}\in \mathbf{R}$  s.t.  $\mathfrak{b}\not\in \mathbf{B}$ .



(d) Condition 3, successful Termination.

Figure 5: Satisfiability of Conditions. [Van12]

## Track Y

# One Paper, Two Paper, Red Paper, Blue Paper; and Other Fun Games for Children

#### Red i Removal with Artificial Retinal Networks Dr. Tom Murphy VII Ph.D.\*

Keywords: computational photography, image processing, generalized photoshop, artificial retinal networks, types

# A Proof of the Twelve-Color Theorem: Hey, Nobody Bothered Before Y. T. Boveck and Victoria V. Varg-Mack

Keywords: twelve colors, planar giraffes, time travel, drivel, fonts are ugly in the future

### 3. Visually Identifying Rank

#### David Fouhey, Daniel Maturana, and Rufus von Woofles

Keywords: perceptual organization, vitamin rank deficiencies, egalitarianism in the PSD cone, PAC bounds for SVDs, class-conscious norms

#### 4. Transparency Report

#### Three Letter Agency

Keywords: transparent, invisible, see-through

## Red i removal with artificial retinal networks

Dr. Tom Murphy VII Ph.D.\*

1 April 2015

#### Abstract

We present a GPU-accelerated means for red i removal in photographs.

**Keywords**: computational photography, image processing, generalized photoshop, artificial retinal networks, types

#### 1 Introduction

When light—such as the bright flashbulb of a camera strikes the human eye, it illuminates the retina. Some of that light bounces back out of the eye, but most of it stimulates neurons in the retina to produce electrical signals. These signals stimulate other neurons to which they are connected, and so on, until the brain (which is technically part of the eye) perceives an image, as a two-dimensional array of neurons with different activation levels. Humans often use these images to sense the world, for example, in reading research papers.

This research paper concerns a particular feature of this process, which is that humans are able to view an image and ignore certain details of it. For example, Figure 1 contains a printout of an image file of a photograph of a television displaying a recorded video of an actor. The video contains a superimposed eye in the corner, the logo of the network CBS. Most viewers are not tormented by this everpresent eye staring at them! In fact, most viewers are able to completely ignore the eye, and view the scene as though it didn't contain the stimulus, even if details such as the actor's sweatshirt's collar pass beneath the stimulus and are occluded by it.

Some stimulus is more everpresent than others. The Clay Mathematics Institute lists among its unsolved *Millennium Prize* problems the "red i removal problem." This concerns the removal of stimulus (a red letter "i") from images (Figure 2). The problem is particu-



Figure 1: Q. Who watches the TV watchers? A. CBS's all-seeing eye.

larly difficult because the information occluded by the i is completely gone, and because the authors of papers about the problem are persistently agitated because it seems like the letter should be capitalized.

In this paper I show how red i removal can be solved in certain specialized cases, using an artificial retinal network patterned after the brain contained within the human eye. Training this artificial retinal network is feasible on a single powerful desktop machine. Both training and execution of the model (a mere 400 megabytes) are GPU accelerated. The model presented in this paper was trained in about 3 days, and executing it in parallel on a suite of images takes about 100 milliseconds per image.<sup>1</sup>

#### 2 Artificial retinal networks

As I expertly foreshadowed in the previous section, an artificial retinal network works just like the brain inside a human eye. The retina is itself a rectangular 2D array of neurons, which turn photons into IEEE-754 floating point values between 0.0f and 1.0f. Behind this

<sup>\*</sup>Copyright © 2015 the Regents of the Wikiplia Foundation. Appears in SIGBOVIK 2015 with the increasingly askance visage of the Association for Computational Heresy; *IEEEEEE!* press, Verlag-Verlag volume no. 0x40-2A. 0.00 Australian Neo-Dollars

<sup>&</sup>lt;sup>1</sup>Source code is available on the World Wide Web at: http://sourceforge.net/p/tom7misc/svn/HEAD/tree/trunk/redi



Figure 2: An image of an Enigma machine rotor with a red i superimposed. Solving this instance of the red i removal problem would mean producing an image without the red i. One way to do this would be to steal a floppy disk containing an original, unimposed image of the rotor, from someone in possession of it, for example the paper's author.

is another 2D array of exactly the same size, except the pixels are in a weird jumbled order, and then another layer. This series of layers is known as the optic nerve. Finally, the brain perceives the image as an array of pixels, again of the same size (Figure 3).

It is easy to reconceptualize this process as an array of pixels undergoing several transformations. Obviously the story is more complicated: Humans see in color, so each pixel is actually three different nodes, one for red, green and blue. In fact, since some scientists hypothesize of certain "superseers"—that is, people who can perceive more than just the three wavelengths of light—we actually allow an arbitrary number of nodes per pixel. In this work, we used N = 4.

In a real human eye, each node is fed inputs from every node in the previous layer. For computational efficiency, in this work we allow only 64 inputs to each node from the previous layer. Because we suspect that layers are spatially related, a node is always connected to its *neighborhood* in the previous layer (each node from the 9 pixels within Manhattan distance 1). The rest of the inputs are selected randomly from a Gaussian distribution, as long as the samples fall within the image (using rejection sampling—the sides and corners do not "wrap around"). By the way, the images are always 256x256, because numbers that are a power of two are faster.<sup>2</sup> The connection from one node to another





Figure 3: How eyes work, and thus, artificial retinal networks.

is modulated by a *weight*, again an IEEE-754 floating point number. A node outputs the sum of its input values, passed through a smoothulator, specifically the one found in Gray's Anatomy (the book, not the TV show),

$$\frac{1}{1+e^{-v}}$$

This function is *biologically plausible*.

We learn by backpropagated stochastic gradient descent, like babies do. Specifically: The network is presented with an image on its retina, and then we run the floating point values through the layers, summing them up and applying the smoothulator function, to produce a final image within the brain. Like a baby, it compares this image to what it expected to see, node by node. Where each node does not agree with the image, the error is computed. The baby propagates the partial derivative of the change in error with respect to the change in stimulus to the previous layer proportional to its weighted impact; fortunately the smoothulator has a simple derivative that is easily computed at a point from its output values. Error is not propagated into the real world (i.e., by sending light off of the retina back to the physical object that created the stimulus: that would be ridiculous).

#### 2.1 Training data

One of the insights of this paper is that although artificial retinal networks require a lot of data to train, for certain problems the training data can be easily generated. For the red i removal problem, we begin with a corpus of about 4,000 images that were scraped from Google Image Search. Scraping images is easy; one just needs to list a bunch of queries for things that babies would want to view in order to learn what the world looks like. In this experiment I used terms such as [snakes], [dog on skateboard], [guitar], [stonehenge] and [superyacht]. Following this, I manually cleaned

In the human eye, powers of ten are faster, because humans have ten fingers.
the training data. I deleted images that were not photographic (drawings, etc.; for example, most images of guitars are actually 3D rendered cartoon guitars, fantasy images of guitars on fire, the Guitar Hero logo, and so on) or that were *too*, uh, pornographic (most queries for things that can have sex, like tapirs, contain prominent images of the things having sex). These are not appropriate for babies.

All images are cropped to a square and resized to 256x256. Then we generate training instances: An input image and the expected result. An image that does not contain a red i should just be transformed into the image itself (indeed, when we peer directly into the brain of a baby looking at a TV show, we find a region of the brain where the TV show is clearly visible). It is also easy to generate instances of the red i removal problem along with their solutions—we simply put a red i randomly on the source image and keep the destination image unchanged. In this way, we can easily generate a large amount of training instances (in actual practice, this procedure had a small bug; see Section 3.1). One unexpected phenomenon is that I had to be careful to remove images that already contained a red i, like many images of casinos, which are often called "CASINO".

In order to coax networks into recognizing the i, we also place an i into the 4th color channel in the same position in the *expected output*. This is an invisible color channel which we discard, and which is always zero in the input. In essence we giving a hint to the eye's brain that it should not just remove the red i, but it should also *perceive* it. I have not performed enough experiments to know if this is helpful.

For repeatability's sake, important constants used in this experiment: There were 2 hidden layers. Gaussan samples were produced with a standard deviation of 16 pixels. The red i was rendered in Comic Sans, at a height of 80 pixels. I used a variety of learning rates, including an expontentially decreasing one (the standard advice of 0.05 is too large for constant learning rates on this kind of task, and limits the sharpness of resultant images).

#### 2.2 CUDA, SHUDA, WUDA

Because we are working with graphical data, we should use the Graphics Processing Unit of the computer, not its Central Processing Unit (we are not processing centers). I implemented high-performance OpenCL kernels for each phase of training: The *forward* pass (signals flowing from the retina to the eye's brain), the *backpropagation* step (when the eye computes the error and partial derivatives) and the *weight update* step (when

the eye rewires its neurons so that it sees the right thing next time). The phases have different parallelism constraints. Because the connectivity is sparse, we represent both forward and inverted index maps, which are decoded on the GPU. We take care to only load a single layer of the retinal network into the GPU's RAM at once, to enable very large models, but we run many training instances in parallel for a single round. Some other operations, like the preparation of training data, are performed on the CPU. These are also frequently done in parallel, using C++11's new std::thread with some crazy-ass wrappers to allow them to function in mingw32's 64-bit gcc port. On a good day, training uses all 6 CPU cores and all 2800 GPU cores and about 14 GB of RAM and warms the home office like a 1kW space heater.

### 3 Results

After 4 rounds of training, the network produces an excellent-looking image that could be a *Cure* album cover, regardless of the stimulus cast upon its retina (Figure 4).



Figure 4: Result after 4 rounds of training. Looks great, and there is no red i to be seen, but it loses some points for not resembling the input image at all.

It's not long before the network learns that it should not produce the same result for every input, and the output starts to mimic the input. These images look sort of like the world viewed through frosted glass (Figure 5), simulating how a baby first learns to see the world through the 1cm bulletproof Lexan of its translucent BabyLearn incubation cylinder.

Soon thereafter, the network begins to converge on

something like the identity function, as this drastically reduces error (even if some error is incurred by the persistence of the red i). Left overnight (about 9,000 rounds), we start to see the network both produce images much like the original (perhaps through a hip "vintage" Instagram filter), as well as removing the red i stimulus (Figure 6).

#### 3.1 Evaluation

With a further 30,000 rounds of training, the output images sharpen and lose their Instagram quality (maybe only a small amount of "grain"), and the i is still successfully removed. However, since we've now made many passes over each image in the training set (and the model has about 100,000 degrees of freedom), it is certainly possible that we've simply overfit to this set of images (that is, that the baby's eye's brain is simply memorizing the i-free images and then recalling the one that looks closest to the stimulus). To evaluate fairly, we need to apply the model to totally new images that it was not trained on. These are called "eval" images.

Firing this up, I observed that the model successfully reproduced eval images that did not contain a red i; this is good because it means that it is not simply memorizing the training set images. I then started placing red i stimulus on the images with the mouse, and my heart sank: It wasn't removing the red i at all! Dejected, I tried loading up the training images and putting a red i on them—it also did not remove the i, which did not make sense! Even for babies! Eventually, I discovered that the red i would be removed, as expected, but only when the i was in a handful of very specific locations. This was found to be a bug in the random i placing code; can you find it too?

```
uint8 x_dice = seed & 0x255;
seed >>= 8;
uint8 y_dice = seed & 0x255;
```

As a result, there are only 16 different possible x coordinates, and same for y. Nonetheless, this is still 256 different i locations that work, which implies considerable generality is possible. Due to Draconian SIGBOVIK deadlines, I have not yet been able to test a debugged training procedure.

Once the evaluation code only places an i at expected locations, the artificial retinal network works well (Figure 7)!

### 4 Conclusions

We find that the supposedly impossible red i removal problem is in fact solvable, at least in some forms, using artificial retinal networks. There are some limitations of the current model:

- It has only been tested to remove the letter i when it is rendered in bright red, in 30 point Comic Sans.
- It probably also removes letters like j, but maybe also in some other fonts, which is a sword that cuts both ways.
- Due to a bug, the red i must be at a position whose coordinates are exactly  $\langle 12 + x_0 + 4x_1 + 16x_2 + 64x_3, 12 + y_0 + 4y_1 + 16y_2 + 63y_3 \rangle$ , for  $x_j$  and  $y_j$  in  $\{0, 1\}$ .
- It automatically and non-optionally applies Instagram-style filters.

This technique can probably be applied to other image processing problems, for example, J peg dequantization. Here, we take an image and badly quantize it (for example, to 4 bits per color channel), and the training instance consists of the quantized image as input and the original image as the expected output; the retinal network learns how to fill in detail. Figure 8 shows the early stages (about 4000 rounds) of training such a model.

A related, still unsolved problem is "red i reduction"; here we do simply remove the i but replace it with a smaller i. For example, we could replace a capital I with a lowercase one, or replace a lowercase 30pt Comic Sans i with a lowercase 29pt Comic Sans i. This is an offshoot of the text ure compression field, which seeks to make the text "ure" smaller wherever it appears.

Biologically-inspired computer algorithms hold many wonders for those that seek to tap into the limitless potential of the 85% of the human eye's brain that is currently unused. Perhaps humans even contain graphics processing units!

For higher-fidelity images and source code, please consult http://tom7.org/redi.



Figure 5: Result after 80 rounds of training, with the input image at the top and the signal proceeding downward through two hidden layers. The hidden layers aspire to crazy noise-terror glitch art versions of the stimulus as well.



Figure 6: After about 9,000 rounds. Top row is the input image, the second row is the output (no longer showing hidden layers because they all just look like firefly raves); the bottom row shows 4x magnified detail of the region formerly containing the red i. Images are somewhat desaturated and blurry, but the red i is removed. Note how in the right image, the retinal network successfully continued both the horizontal and vertical bookshelves into the occluded region. This is not a trick.



Figure 7: Evaluation on new images after 30,000 rounds of training. Top row is the input image, the second row is the output, and third is 4x magnified defail. The first image (no i) shows the high amount of detail preserved. In the latter two, the i is successfully removed; the quality of the replacement is not perfect, but certainly reasonable.

Figure 8: Evaluation of an early model for J peg dequantization. The model still contains a lot of noise pixels, which sometimes take a long time to converge, but it is already easy to see how quantization artifacts have been reduced (left). Actually, there is no reason why such dequantization must only be applied to J pegs; the right column shows it working on a nice rainbow picture.

## A Proof of the Twelve Color Theorem: Hey, Nobody Bothered Before.

Sixth Grade Class Project for Mr. Blum

Y. T. Boveck Victoria V. Varg-Mack, VI

April  $1\frac{1}{3}$ , 2071

Editor's note: Several days ago, the wreckage of a small time machine appeared in the program committee's office, containing apparently only a copy of the proceedings from SIGBOVIK 2071. Unfortunately, all papers but one were burnt beyond recognition. Current speculation holds that the time machine operators forgot to disable the paradox safety interlock, and all the important (potentially causality-violating) papers were destroyed, leaving only this drivel. We're publishing it anyway, sorry.

#### Abstract

Roughly 100 years ago, mathematicians successfully proved the 4-Color Theorem. Widely regarded as one of the most important theorems in graph theory at the time, the 4-Color Theorem states that for all planar graphs there exists an assignment of colors to nobes, such that no two adjacent nobes are assigned the same color, with at most 4 colors used. However, modern-day computers are capable of rendering far more diverse color palettes, and the old 4-color limitation is now largely irrelevant. In this work we extend the old result to support 12-colorings, offer some thoughts on generalization, and leave a conspicuous hole in our proof to support our future work.

#### 1 Introduction

Victoria said I had to write this section, even though she's the only one of us who actually knows how the 4-color theorem proof goes. But luckily I found a proof for the 5-color theorem that made sense, and since having more colors is obviously better, that should work just as good. It goes like this:

Lemma 1.1. All planar graphs have at least one nobe with at most 5 neighbors.

*Proof.* Let N(n) mean how many neighbors a given nobe n has. Then because each edge connects two nobes, the sum of all nobes' neighbors  $\sum_n N(n) = 2e$ . Let's assume all nobes have at least six neighbors. Then  $6n \leq 2e$ .

Next let E(f) mean the number of edges that make up the border of a given face f of the graph. Since each edge borders 2 faces,  $\sum_{f} E(f) = 2e$ . Every region is bounded by at least 3 edges so that means  $3f \leq 2e$ .

If we plug all that into the "Euler's Forumula" that Mr. Blum gave us in class, which says that n - e + f = 2, here's what we get:  $n - e + f \le \frac{e}{3} - e + \frac{2e}{3} = 0$ . But since n - e + f = 2 we end up with  $2 \le 0$ . Then we must have been wrong to assume all nobes have at least six neighbors. That's a "contradiction"!

**Theorem 1.2.** All planar graphs can be colored with no more than 5 colors so that no neighbor nobes have the same color.

*Proof.* Let G mean the graph we're trying to prove this for. Using the lemon I just proved, pick the nobe n that has at most five neighbors and call those  $n_1$ ,  $n_2$ ,  $n_3$ ,  $n_4$ ,  $n_5$  in whatever order you want, but remember the order! Let G' mean the smaller graph you get by taking out n, which of course is still planar. Because G' is smaller, we already know with "induction" that G' can be 5-colored. [That step seemed kinda weird to me but Victoria said it was legit so please don't take points off.]

Now we're gonna assume G can't be 5-colored. For this to be true, then each  $n_i$  from 1 to 5 must all have different colors, or else you could just pick the missing one for n. Let's think about the sub-graph that has only the 2 colors matching  $n_1$  and  $n_3$ , call it  $G_{13}$ . If the graph is disjoint, meaning  $n_1$  and  $n_3$  are in two separate parts, then you would be able to re-color the graph to make  $n_3$  have color 1, so you can paint n with color 3. Therefore  $G_{13}$  must be connected. You can make the same argument for  $G_{24}$  to be connected, but suddenly that doesn't make any sense, because a path that keeps  $G_{24}$  connected would have to intersect the connected  $G_{13}$ !

So now, even if the 5-coloring of G' gives all different colors to  $n_1$ ,  $n_2$ ,  $n_3$ ,  $n_4$ ,  $n_5$ , you should be able to re-color one of the  $n_i$ s so you can have a spare color to give to n. That means you can 5-color G.  $\Box$ 

Nice! Hey, that wasn't so bad.

#### 2 The 12-Color Theorem

In the previous section, Y.T. et al. outlined the prior work in the field. Now we will make our main contribution; namely, to extend the 5-color theorem reviewed above to allow for 12-colorings of arbitrary planar graphs.

**Theorem 2.1.** Given an arbitrary planar graph G, there exists an assignment of no more than 12 colors to the set of nobes N(G) such that no two neighbouring nobes are assigned the same color.

*Proof.* Using Theorem 1.2, generate a 5-color assignment for G. As 5 is less than 12, this assignment suffices.

Corollary 2.2. If G has at least 12 nobes, then all 12 colors may be used.

*Proof.* First we will prove the case for a smaller number of colors c < 12, by induction on c. Assume a graph G with c or more nobes, and an existing assignment of c - 1 colors in which all colors are represented, such that c < 12. The pigeonhole principle states that there must exist two nobes  $n_1$  and  $n_2$  with the same color. Simply assign the cth color to  $n_2$  in the new coloring.

Next for the case c = 12. Given a graph G with 12 or more nobes, there must exist an assignment of 11 colors in which all colors are represented. The pigeonhole principle states that there must exist two nobes  $n_1$  and  $n_2$  with the same color. Assigning the 12th color to  $n_2$  causes all 12 colors to be used.

An example application of our algorithm is depicted in Figure 1.

### 3 Conclusions and Future Work

In this paper we reviewed historical developments in the field, with a particular focus on the proof of the 4-Color Theorem 5-Color Theorem; and we presented our main contribution, a constructive proof of our new 12-Color Theorem based on the assumption of existing 4-colorings 5-colorings of an arbitrary planar graph G.

The most significant limitation of our work is that a generalized version of our proof only applies for C-colorings when  $C \leq 12$ . In future research, we plan on extending our theorem to support ever greater values of C. We hope the need for additional funding to study such advanced open problems is self-evident.



(a) Make a 4-color of your graph first.



(c) Repeat that seven more times to get a 12-coloring!

(b) Choose a nobe and color it different.



[d] If you had 51 different colors and wanted to use them all, it would look like this. However, we are leaving a proof of the existence of generalized 51colorings to future work.

Figure 1: Mr. Blum said we needed to have some pictures in our paper, so we pretended the USA was a graph and colored it like our algorithm says.



Paper 10: A Proof of the Twelve-Color Theorem

### Mr. Blum, New Pittsburgh Middle School Rating: :( Confidence: 4/4

This project makes a well-meaning, but ultimately entirely unconvincing, attempt at proving an interesting theorem in computer science. In the early twenty-first century, when the four-color theorem was still considered exciting, as opposed to something that all schoolchildren are taught from an early age, this might have been a reasonable starting point for sixth-grade work. Unfortunately, my standards are higher than this. I would have been more impressed if Y.T. and Victoria had started with a more recent and interesting result, such as the 2068 paper of Blum et al. (no relation) showing that P = NP.

Of course, as this class is "United States History: The 2017 Burrito Wars to the Present Day", none of the above has any bearing. Using our school's standard grading scheme of :) to :(, I assign this project a :(

# Visually Identifying Rank

David F. Fouhey, *Mathematicians Hate Him!* Daniel Maturana, *Random Forester* Rufus von Woofles, *Good Boy* 

**Abstract**—The visual estimation of the rank of a matrix has eluded researchers across a myriad of disciplines many years. In this paper, we demonstrate the successful visual estimation of a matrix's rank by treating it as a classification problem. When tested on a dataset of tens-of-thousands of colormapped matrices of varying ranks, we not only achieve state-of-the-art performance, but also distressingly high performance on an absolute basis.

Index Terms—perceptual organization; vitamin and rank deficiencies; egalitarianism in the positive-semi-definite cone; PAC bounds for SVDs; class-conscious norms



Fig. 1. What are the ranks of these matrices? Which ones are rank-deficient? In this paper, we investigate how one can guesstimate the rank of a matrix from visual features alone. See footnote on page 2 for answer.

#### **1** INTRODUCTION

Consider Figure 1(b): what is the rank of the matrix? Most people are confused. Some might hazard a guess. A select collection of professors might say "3." The mystery of how professors can visually estimate the rank of matrices from as little as a brief glance at a jet-colormap rendering has puzzled researchers in neuroscience, philosophy, mathematics, and computer science for decades.

The rank of a matrix M reveals a great deal. By definition, it tells us how many linearly independent columns the matrix has; surprisingly, it also tells us how many linearly independent rows the matrix has, and if that does not get you excited, I do not know what will. If we think of M as an operator, the rank tells us about the dimensionality of its output, and thus for a square matrix, whether M is invertible.

In this paper, we show how to identify the rank of a matrix from an image alone. In contrast to past work on guaranteed solutions to matrix rank computation

 All authors are with The Robotics Institute, Carnegie Mellon University.
 Send us fan mail at: Neurotic Computing Institute c/o D. Fouhey, A.B. M.S. EDSH 212
 5000 Forbes Avenue that require access to the matrix, our work gives guarantee-free solutions that can operate on only an colormapped version of a matrix. By treating matrix rank as an image classification problem, we are able to consistently achieve distressingly high performance –  $\approx 40\%$  accuracy on 10-way classification;  $\approx 80\%$ accuracy on rank-deficient/not-rank-deficient binary classification. In subsequent experiments we show the following: 1) Our method can identify what matrices seem low rank, and why; 2) Our method is easily extended to structured prediction; 3) That activations of our network can be even used as a feature for semantic image classification with non-embarrassing performance (20.9% on Caltech 101 with 15 samples).

#### 2 RELATED WORK

In this work, we tackle two problems concerning a square matrix  $\mathbf{M} \in \mathbb{R}^{n \times n}$ . The first is a binary classification problem: is  $\mathbf{M}$  full-rank? The second is a *k*-way classification problem: what is the rank of  $\mathbf{M}$ ?

Many approaches exist for solving both problems. In the binary case, for instance, note that a square matrix is full rank if and only if its determinant is nonzero. This leads to a straight-forward way to check for rank deficiency. Similarly, if we let  $\mathbf{U}\Sigma\mathbf{V}^T = \mathbf{M}$  be the singular value decomposition of  $\mathbf{M}$  (i.e.,  $\Sigma_{i,i} = \sigma_i$  where  $\sigma_i$  is the *i*th singular value of  $\mathbf{M}$ ), then the rank is the number of non-zero singular values. This permits checking not only for rank deficiency but also calculating the rank.

While these sorts of approaches enable the accurate solution of both questions, they (a) require access to the matrix itself (as opposed to a screen capture or printout) and (b) have time complexity greater than  $O(n^2)$ . SVD computation has complexity  $O(n^3)$  and determinant calculation is  $O(n^3)$  with Bareiss [1] or  $O(n^{2.807})$  with Bunch and Hopcroft [2]. Our work aims to fix these gaps.

Our method requires only access to a visual representation of the matrix, and thus answers the purely

Pittsburgh, PA 15213



Fig. 2. Examples of matrices of various ranks. Top row: random instances; Bottom row: archtypical examples of each rank, determined by the most confident classification examples from a pool of 1,000 matrices according to a classifier.

*visual* way of computing rank as opposed to the *mechanical* way of computing rank. When a professor says a matrix looks rank-deficient, she is probably not doing an SVD, but instead using some visual smell-test (akin to the notion of direct perception as proposed by psychologist J.J. Gibson [3]); we seek to emulate this astounding ability.

Our method is  $O(n^2)$ . Feature extraction is only dependent on the number of pixels for all methods and thus  $O(n^2)$ . If we are doing binary classification, it is O(1) and thus the method serves as a guaranteefree quadratic-time rank-deficiency test. If we do *n*way classification, it depends on the method, but is arguably O(1) for random forests, which most of our methods use.

We acknowledge that our work gives no guarantees, but computer vision has a long history of extraordinarily successful algorithms that may not always be right. The Random Sample Consensus algorithm [4], for instance, can give no guarantees about its performance on any individual problem instance. However, it works extraordinarily well in practice, and the authors have taken it all the way to the proverbial citation bank with a well-deserved  $\approx 10,000$  citations. Similarly effective methods include Simulated Annealing, Iterative Conditional Modes (ICM) [5], and many others. Our method may not be as successful, but as presented in Table 1, our method is surprisingly effective and has a certain je ne sais quoi.

Our approach of neural-network based approaches to linear algebra is not itself novel. However, previous approaches (e.g., [6], [7], [8], among many others) require direct access to the matrix itself. Our approach, on the other hand, only gets access to an colormap of the matrix.

The natural complement to the thematically-related related work section (as above) is the alphabeticallyrelated related work section introduced in Fouhey and Maturana's seminal work on celebrity-themed learning [9]. In this paper, we extend this to a word-based

#### TABLE 1

A comparison of ways to check whether a matrix is rank deficient. We evaluate methods on their time complexity, their success rate, whether there is an easy extension to *n*-way rank calculation, and their Je Ne Sais Quoi.

Method	Complexity	Success	Multi-class	Je ne sais
Name	(Time)	Rate	Extension	quoi
SVD	$O(n^3) \\ O(n^{2.807}) \\ \mathbf{O}(\mathbf{n^2})$	100%	Yes	Minimal
Det.		100%	No	Kinda
CNN		78.6%	Yes	<b>Tons</b>

related work section. A highly related technique is the rank transform proposed by Zabih and Woodfill [10]. This method replaces each pixel by its "neighborhood rank" to achieve invariance to monotonic illumination differences. We employ a related technique, Local Binary Patterns [11] to extract features for our classifiers. Also related are learning-to-rank algorithms such as support vector ranking [12].

#### **3 TECHNICAL APPROACH**

We now introduce the method in simple English to illustrate its simplicity. We take a matrix, visualize it as a picture (like a.png), and feed it into a standard image classification pipeline. More formally, we create a fixed-length feature representation  $\phi$  of the image, and learn a mapping f that maps the representation to a set of discrete classes. For instance, we might extract standard image features like SIFT as  $\phi$ , and apply a standard technique like Random Forests or SVM to learn an *f*. Similarly, we might train a convolutional neural network (CNN) to predict the rank, serving as both  $\phi$  and f. This classifier is simply trained on a collection of random matrices. We note that one elegant aspect of our method is that rank-deficiency and classification are encapsulated in the same learning formulation.

#### 3.1 Features and Learning Method

In this paper, we apply standard image classification machinery by substituting in various standard fea-

1. Answers first page quiz: a - rank 1; b - rank 3; c - rank 10.

TABLE 2

Quantitative results on visual rank problems. Our paradigm of rank-prediction works surprisingly well across a myriad of features and learning methods.

Learning method $f$	f Random Forest+Engineered			RF + Pretrained		Scratch CNN	Chance	
Feature map $\phi$	All Eng.	Gray SIFT BoW	Color SIFT BoW	LBP BoW	$pool_5$	fc7	Raw Pixels	
10-way Rank Rank Deficiency	38.1% 76.4%	32.5% 73.1%	36.5% 75.3%	31.0% 73.9%	33.7% 75.0%	34.9% 76.3%	43.5% 78.6%	10% 50%
Rana Deficiency	70.170	, 5.1 /0	, 0.070	10.970	, 0.070	10.070	70.070	0070

tures and learning methods for  $\phi$  and f.

**Shallow Learner + Features:** *Features* ( $\phi$ ): The first feature type we use is standard hand-engineered features in the form of a bag-of-words (i.e., histogram) representation over dense SIFT [13] and Local Binary Patterns (LBP) [11]. To quantize SIFT, we build a codebook with k-means; each extracted SIFT feature is represented by the nearest cluster center (i.e., hard assignment). Thus, each image is mapped to one or more histograms of codewords; we concatenate histograms when using multiple representations. We also experiment with using the responses of a standard convolutional neural network – Alexnet [14] – pretrained on the Imagenet dataset [15]. We use the standard pool<sub>5</sub> and fc<sub>7</sub> features.

*Learning Methods (f):* We work with random forests [16] although our method is entirely generic. In this method, an ensemble of decision trees is trained independently. During learning, splitting occurs on a random subset of features and occurs until a minimum number of samples is in a leaf. Whenever training, we do 5-fold cross-validation on the training data and select the values for both parameters (number of features considered, minimum node size) that give maximum mean performance.

Deep Learning: In keeping with the spirit of the deep learning times, we train a CNN to map directly from pixels to matrix rank. We refer to this as a Scratch CNN in the experiments since it is learned from scratch. Our experiments use a small amount of data, so we adapt a network designed for the MNIST dataset [17] that appears in the examples for [18]. Starting with all images resized to  $60 \times 60$ , our network has architecture  $C(5,20) \rightarrow P(4,3) \rightarrow C(5,50) \rightarrow$  $P(4,3) \rightarrow C(4,500) \rightarrow R \rightarrow \text{softmax}$ , where C(k,n)denotes a convolutional layer with n filters of size  $k \times k$ , P(k, s) is max-pooling over a  $k \times k$  region with stride s, and R is a rectified linear unit. Empirically, we found that the more aggressive max-pooling than usual helped the network generalize to matrices of other dimensions.

#### 3.2 Implementation Details

We used Piotr Dollar's toolbox [19], Vedaldi et al.'s VLFeat [20], MatConvNet [18], and LIBSVM [21]. *SIFT:* We extract and quantize SIFT on both the gray image and each of the R, G, and B channels separately; each codebook has 256 entries and one codebook is

generated on training data per channel. The codebooks are learned once on the  $10 \times 10$  training set. *Scratch CNN:* We use a learning rate of  $10^{-3}$  in a standard gradient-descent+momentum approach and 1M iterations; to prevent overfitting, we use the first iteration to have validation error within 1% of the final validation error.

#### **4 EXPERIMENTS**

We now rigorously evaluate our approaches for visually guesstimating rank-related matrix properties. *Every figure and table in this section represents a true experiment and actual results. We do not mess around.* 

#### 4.1 Dataset

We perform our experiments on a dataset of  $10 \times 10$  matrices, with 2000 examples of each rank  $1, \ldots, 10$ , which we split evenly into train and test. When doing binary rank-deficiency classification, we balance class distributions by downsampling the rank deficient class. We generate these matrices by first sampling a matrix **M** with entries uniformly and independently sampled from the interval [0, 1]. We then compute its SVD  $\mathbf{M} = \mathbf{U}\Sigma\mathbf{V}^T$  and set  $\Sigma$  to  $\Sigma$  but with the  $r + 1, \ldots, n$ th entries to 0 and compute  $\mathbf{U}\tilde{\Sigma}\mathbf{V}^T$ .

We convert each matrix to a  $100 \times 100$  image, which we store as a PNG. This is done in MATLAB by calling the underlying colormapping functionality used by imagesc and then upsampling with nearest neighbor. In this paper, we primarily use the traditional and often criticized jet colormap, but we also experiment with two linear colormaps, copper and bone. All colormaps have 255 possible values and are scaled by the min and max of the matrices (i.e., the default of imagesc, where no absolute scale is imposed). Note that the many matrices of a variety of ranks may map to the same colormap visualization due to both colormap and PNG quantization.

#### 4.2 Experiments – Features

In this section, we ask the question: what visual features are best suited for visually identifying the rank of a matrix? Is color a useful cue? It was argued in [22] that off-the-shelf pre-trained CNN features are an astoundingly effective baseline for any generic vision task – does this include profoundly unnatural



Fig. 3. Confusion matrices and accuracies for different colormaps on the 10-way rank classification problem using dense SIFT and LBP. Note that while there is variation, performance is decidedly above chance across colormaps.

images such as color-mapped matrices? Does learning a specialized CNN work on this task?

We present results in Table 2 showing the performance of various features. In the hand-engineered category, grayscale SIFT seems to perform on par with LBP; adding color considerably improves performance; and using all features does the best. The pretrained CNN does well despite the giant domain shift with both layers do slightly better than grayscale SIFT. However, in keeping with current results in computer vision, training a CNN from scratch consistently does the best. *Note, however, that all feature and method combinations operate at significantly above chancelevel.* 

#### 4.3 Experiments – Colormaps

One natural question is whether the colormapping scheme affects the visual discrimination between matrices of different ranks. The jet colormap (e.g., Figs. 1, 5) in particular has received a lot of criticism for being difficult to interpret in practice by humans. Linear colormaps (i.e., smoothly varying from one color to another) in theory make for easier interpretation by humans. We see whether this holds true for computers as well. We compare the jet colormap (named for its origin in astrophysical fluid jet simulation) with copper and bone. The etymology of copper is – we hope for the reader's sake – obvious; bone is so named because it looks somewhat like an X-ray and is popular because it lets researchers like us try to pretend to be brain-surgeons.

We run our learning method on matrices with a variety of colormaps and report 10-way classification results in Fig. 3 and 4. Generally, jet does the best. The only representation on which it does appreciably worse is the pre-trained CNN; we hypothesize this is because the linear colormaps produce more natural images, whereas the jet colormap's outputs look like noise. Using grayscale SIFT, the results are roughly comparable, which is somewhat surprising as jet is known to convert poorly to grayscale. Nonetheless, while these differences exist, one consistent pattern is that the proposed method works surprisingly well across all colormaps.

Fig. 5. Failure cases: some deceptive matrices with their (P)redicted and (A)ctual ranks, selected from the most confident mistakes of a RF classifier using dense SIFT and LBP features.

#### 4.4 Experiments – Cross Domain

One recent pressing concern in the computer vision community is the biased nature of datasets: models learned on one dataset might not perform even reasonably on another, as reported in [23]. In our case, one might wonder whether a model learned to predict the rank of a  $10 \times 10$  matrix (with a fixed set of ranks  $1, \ldots, 10$ ) can generalize to matrices of different sizes (e.g.,  $30 \times 30$ ). To answer this, we train a 10class random forest on square matrices of dimensions 10, 15, and 30, and test them on different sizes; bagof-word features are generated using the  $10 \times 10$ matrix codebooks. These new matrix images have dimensions  $150 \times 150$  and  $300 \times 300$  respectively to maintain scale for the SIFT features. CNNs require a fixed input, and so we cannot apply this scaling trick to them.

We train a model to predict ranks  $1, \ldots, 10$  for all matrix sizes involved and report results in Table 3. Our method does surprisingly well, performing at around  $2.5 \times$  chance-level when training on  $10 \times 10$  matrices and testing on  $30 \times 30$  matrices and vice-versa. The scratch CNN generalizes well, with the exception of the  $30 \times 30$  scratch CNN on  $10 \times 10$  data, which operates at chance level. This is poor generalization as opposed to a bad model to start with: the same model gets 49.7% when testing on  $30 \times 30$  and 14.6% on  $15 \times 15$ . We believe generalization could be improved by developing an architecture that would enable the row-to-pixel ratio to be constant.

#### 5 DISCUSSION

The success of such a simple approach raises a number of questions, but our method also enables answer to some of these. For instance, we can see what makes a matrix smell rank deficient by analyzing the learned relationship between  $\phi$  and f. We now discuss a few of these questions as well as extensions.

## 5.1 What does an archetypical rank-*k* matrix look like and which matrices are tricky to classify?

We can answer each of these questions by looking at the classifier scores; by looking at the most confident



Fig. 4. What colormap is best for predicting matrix rank? (Left to right: jet, bone, copper). While Jet has been criticized widely compared to linear colormaps, it produces the best results with color sift and the from-scratch CNN

 TABLE 3

 Cross-domain performance: We report the accuracy of the methods on 10-way classification. Although chance on this task is 10%, most of our methods perform substantially better than chance.

Train	Test	R	Random Forest+Engineered				retrained	Scratch CNN
Dim.	Dim.	All Eng.	Gray SIFT	Color SIFT	LBP	$pool_5$	fc7	Raw Pixels
	$10 \times 10$	38.1%	32.5%	36.5%	31.0%	33.7%	34.9%	43.5%
$10 \times 10$	$15 \times 15$	33.7%	31.5%	33.5%	27.3%	25.7%	26.1%	37.9%
	$30 \times 30$	25.9%	19.1%	25.3%	19.4%	17.7%	17.5%	24.1%
$\begin{array}{c} 15\times15\\ 30\times30 \end{array}$	$10 \times 10$	33.0% <b>25.8%</b>	28.1% 22.7%	32.0% 23.8%	26.5% 21.6%	13.9% 11.5%	14.4% 11.8%	<b>34.1%</b> 10.0%

mistakes of the classifier, we can find the most rankdeceptive matrices. We present some archetypical matrices in Fig. 2 according to RF classifier using all features. While the rank 1 matrix archetype is understandable, ranks 2 and up seem inscrutable. Nonetheless, the model is perfectly confident in its assessment of these matrices and is correct a surprising amount of time. Fig. 5 shows the model's confident mistakes. On the left, for instance, is shown a rank-1 matrix with not too much apparent inter-row/column similarity that was mistakenly predicted to rank 3 by the RF.

#### 5.2 What parts of matrices tell us rank?

Given our bag-of-words model, we can answer this by figuring out which codewords help the most in predicting rank as well as their sign (i.e., which codes are most associated with rank-1 rather than rank-10). We solve both by learning a  $L_2$ -regularized logistic regression model to predict Rank-i or Rank-j, which we solve with LIBLINEAR [24]. The regularization parameter  $\lambda$  is selected via 5-fold cross-validation to give best average performance. The coefficients of the model w in terms of magnitude and sign indicate which codewords are indicative of rank deficiency.

We can visualize the informative regions of matrices by replacing pixels with the weight vector of their associated codewords. We show a few examples of this for low rank and high rank matrices using *grayscale* SIFT in Fig. 6. For rank 1, the regions associated with low rank have low frequency, and the codewords associated with high rank occur mainly at the sharp transition from the penultimate and blue column to the last column. The other ranks are a bit harder to



Fig. 6. A visualization of what makes a matrix look rankdeficient according to gray-scale SIFT. We train a logistic regressor to predict rank-*k* vs. full rank and plot weight-vector coefficients onto the image wherever the codeword appears. Blue is low rank, red high.

interpret, although the one can note the most strongly low-rank regions correspond to flat regions.

#### 5.3 Can We Solve Structured Tasks?

So far, our approach of doing mathematics by learning has only been applied to classification problems. In-





spired by our success in visual rank estimation, we are currently exploring the application of our framework to structured outputs, such as matrices.

In particular, we consider matrix multiplication and inversion, where for centuries mathematicians have relied on hand-crafted, shallow methods. Again, keeping with the times we propose to replace these methods with visual deep learning. To this end we designed a deep learning architecture, differing only in the input for each task: for the multiplication task we used two  $M \times M$  concatenated multiplicands as input, whereas in the inversion task there is a single  $M \times M$  input. The input is connected to two fully connected layers using ReLU nonlinearities of 512 hidden units each, followed by a fully connected  $M \times M$  output layer with no nonlinearity. Dropout regularization was used in all layers. We generate  $5 \cdot 10^5$  training examples for each task. In both cases we use  $3 \times 3$  matrices with each entry independently sampled from a uniform(0,1) distribution as input, and their "true"<sup>2</sup> product and inverse as outputs.

We then use this data to train the network with stochastic gradient descent on a mean square error (MSE) loss for 100 epochs. Some qualitative predictions on unseen data are shown in Figures 7 and 8. We found the multiplication task to be easily solved by our network architecture, but the inversion task proved much more challenging, as shown by the higher MSE values. We note that this is analogous to humans taking Linear Algebra 101.

#### 5.4 Can This Work On Real Data?

One advantage of our method is that it does not require access to the matrices themselves; but what if we only have a picture of the colormapped matrix? As a proof of concept, we took a cell-phone picture of each part of Fig. 1 of this paper, as shown in Fig. 9, left. We cropped out the matrix from the cell phone picture, as shown in Fig. 9, right. We then resized



Fig. 8. Examples from our deep visual matrix inverse net.

1 (92.8%) 10 (48.1%) 10(45.5%)

Fig. 9. Results on cropped images from cell-phone pictures of a computer monitor. (Left) sample pre-cropped image; (right) cropped images, their predicted rank, and posterior from the scratch CNN.

it and sent it through our scratch CNN. The rank 1 matrix was classified correctly, but both the rank 3 and rank 10 matrix were classified as rank 10. We note, however, that all images have perspective distortion that the CNN did not see at training time.

#### 5.5 Does the matrix rank network generalize?

In our experiments, we confirmed the reports of [22] that one can use neuron activations from a network pretrained for classification as a strong feature for a variety of tasks; but can we use do the reverse? In other words, can we use activations in our scratch CNN as a feature for image classification?

To evaluate this, we tested our method on the Caltech 101 dataset [25]. We used the concatenated features from the last and second-to-last layers of the rank network (i.e., the softmax responses and the halfwave rectified feature map immediately before) as a feature representation. We then trained a multiclass SVMs (1v1, linear kernel) on top of these representations. We report results in Table 4; results are averaged over 1K random samplings of train sets; for test, we use an equal number per-class. While far from state-of-the-art, the numbers are respectable given that the underlying feature representation was trained to estimate matrix ranks.

#### 6 CONCLUSIONS

In this paper, we introduced a new problem – visual rank estimation - and demonstrated that it is feasible

2. At least according to our matrix library.

TABLE 4 Results on Caltech 101, training a linear SVM over responses from our scratch rank CNN. Chance on this dataset is  $\approx 1\%$ .

# Samples	5	10	15	20	25
Accuracy	12.6%	17.7%	20.9%	23.3%	25.1%

using conventional image classification approaches. Our approach is simple and obtains alarmingly high performance. More importantly, our features also conveys understanding by showing us why some matrices just look low rank and what matrices have surprising rank. We have additionally demonstrated future directions in the form of structured prediction and have demonstrated that our rank predictor CNN can serve as a generic image feature.

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David F. Fouhey David F. Fouhey received an A.B. from Middlebury College in Moose Watching in 2011. He is currently a Ph.D. student at the Robotics Institute at Carnegie Mellon University. He likes long walks, Edward Hopper, macchiatos, Jaffa Cakes, and, above all, kvetching. In his copious spare time, he sends fake announcements to the New York Times' Wedding Section. He and his colleagues were awarded the People's Democratic Choice Award at SIGBOVIK 2013.



Daniel Maturana Daniel comes from Chile. Daniel likes Eat'n Park, bicycling, recycling, and Pabst Blue Ribbon. You won't believe the one weird trick that credit card companies hate that Daniel uses to make money at home thanks to Obama lowering 10-year mortgage rates! He and his colleagues were awarded the People's Democratic Choice Award at SIGBOVIK 2013.



Rufus von Woofles Rufus von Woofles is a good boy, isn't he. Yesh he is. Rufus obtained his DoD (Doggy Obedience Diploma), First Class, from Muddy Paws University. Rufus is currently the PI of CHOCOLATE Lab at Carnegie Mellon University, where he leads research on predicting pizza-delivery-man appearance. Rufus likes wagging his tail and belly rubs. Rufus was awarded the People's Democratic Choice Award at SIGBOVIK 2013, but he tore it up.

### Transparency Report

#### United States Three Letter Agency

#### 1 April 2015

Here at Three Letter Agency, we care deeply about transparency. We have implemented a transparency policy carefully designed to ensure that transparency is at the heart of everything we do. Transparency means that you can set your mind at ease. Our track record proves that transparency is a top priority for us. We are more transparent than air itself. Transparency is our commitment to you. Our mission is to be the most transparent agency on the planet. We worry about transparency so that you don't have to. We take transparency very seriously. We use transparencies in all of our presentations. Finger lickin' transparent. Taste the transparency. Always transparent. We conduct regular transparency audits. We once briefly believed that we were not being transparent, but it was a mistake. A transparent proxy intercepts normal communication at the network layer without requiring any special client configuration, such that clients need not be aware of the existence of the proxy. Transparency keeps you safe. We have a long tradition of transparent processes and outcomes. We make transparency work for you. Transparency is in our DNA. Think transparent. Got transparency? So transparent, no wonder it's number one. Every breath you take, every move you make, we'll be transparent.

# Track L Lunch Intermission

## 1. Burritos for the Hungry Mathematician

### Ed Morehouse

Keywords: burritos, monads, why did i spend my day doing this instead of real work?

### Burritos for the Hungry Mathematician

#### Ed Morehouse

#### April 1, 2015

#### Abstract

The advent of fast-casual Mexican-style dining establishments, such as Chipotle and Qdoba, has greatly improved the productivity of research mathematicians and theoretical computer scientists in recent years. Still, many experience confusion upon encountering burritos for the first time.

Numerous burrito tutorials (of varying quality) are to be found on the Internet. Some describe a burrito as the image of a crêpe under the action of the new-world functor. But such characterizations merely serve to reindex the confusion contravariantly. Others insist that the only way to really understand burritos is to eat many different kinds of burrito, until the common underlying concept becomes apparent.

It has been recently remarked by Yorgey [9] that a burrito can be regarded as an instance of a universally-understood concept, namely, that of monad. It is this characterization that we intend to explicate here. To wit,

a burrito is just a strong monad in the symmetric monoidal category of food; what's the big deal?!

#### 1 The Category of Food

The **category of food**, FÜD, is a full subcategory of the category of stuff, STF, whose objects are the stuff you can eat. A morphism of this category is known as a **recipe**. This category inherits the ambient *monoidal product*: if you can eat a carrot and you can eat a potato, then you can eat a carrot and a potato. The *monoidal unit* in the category of food is nothing,  $\varepsilon$ , which is to be found in many graduate students' refrigerators, typically, tensored with beer.

The monoidal category FüD is *symmetric*: if you can eat a carrot and a potato then you can eat a potato and a carrot. However, it fails to be *cartesian*. We lack the projections: if we have made the mistake of ordering a whiskey sour, there is generally no way to recover just the whiskey. Nor do we have a diagonal natural transformation,  $\Delta(A) : A \longrightarrow A \otimes A$ , giving us two whiskeys for the price of one – alas. For further details on the theory of categorical cookery, see [1].

#### 2 The Tortilla Endofunctor

The category of food supports an endofunctor,  $T : FÜD \longrightarrow FÜD$ , known as the **tortilla endofunctor**. Objects in the image of this functor are precisely those that are wrapped in a tortilla. The action of the functor T on morphisms is to take a recipe and yield a recipe from tortilla-wrapped ingredients to tortilla-wrapped results.

Note that the tortilla endofunctor is, in general, *not* monoidal. Given tortillawrapped rice and beans, it is usually not possible to recover tortilla-wrapped rice and tortilla-wrapped beans. Nor is it always possible to produce a tortillawrapped nothing out of nothing.

#### 3 The Burrito Monad

It is universally understood that a **monad** on a category  $\mathbb{C}$  is comprised of [6] an endofunctor  $T : \mathbb{C} \longrightarrow \mathbb{C}$  and two natural transformations,  $\eta : id(\mathbb{C}) \longrightarrow T$  and  $\mu : T^2 \longrightarrow T$ , known respectively as the monad **unit** and **multiplication**, satisfying the monoid unit and associative laws:

$$(\eta \cdot \cdot T) \cdot \mu \quad = \quad id(T) \quad = \quad (T \cdot \cdot \eta) \cdot \mu \quad : \quad T \longrightarrow T$$

and

$$(\mu \cdot \cdot T) \cdot \mu = (T \cdot \cdot \mu) \cdot \mu : T^3 \longrightarrow T$$

In the case of the burrito monad, the functor in question is, of course, the tortilla endofunctor.

The burrito monad unit takes something you can eat and wraps it in a tortilla, yielding a **simple burrito**, which is both tortilla-wrapped and edible – no mean feat. This constitutes the familiar *insertion of generators* [5]. However, in the case of less-viscous generators, such as guacamole, some care may be required in the insertion, and it is often easier to insert the generator into the monad using a nozzle rather than by the obvious folding map.

The burrito monad multiplication takes a **compound burrito**, that is, something you can eat that is double-wrapped in tortillas, and merges the two tortillas into a single wrapping. This tends to happen spontaneously in the case of an overabundance of the previously-mentioned less-viscous generators, although a similar effect can be achieved mechanically by using some force and the *flattening* function (should we cite the crappy Gabor paper here?) [2].

Now we must check that the monad laws are satisfied:

- **monad right unit law:** This law says that if you begin with something you can eat that's wrapped in a tortilla and you wrap the whole thing in another tortilla, then merge the tortillas, you get back what you started with, as the reader may deliciously verify.
- monad left unit law: This law says that if you begin with something you can eat that's wrapped in a tortilla and you unwrap it, remove the contents

and wrap them in another tortilla, then wrap the result back up in the original tortilla and merge the two wrappings, the effect is again the identity function.

**monad associative law:** This law says that if you have a triple-tortilla-wrapped thing you can eat and you merge the inner two tortillas, then merge the result with the outer tortilla, the effect is the same as if you had merged the outer two tortillas first, and then the result with the inner one.

#### 4 From Burritos, Strength

The burrito monad is in fact strong. A monad  $(T, \eta, \mu)$  on a monoidal category  $(\mathbb{C}, \otimes, I)$  is **strong** if there is a natural transformation,

$$\tau(A, B) \quad : \quad A \otimes T(B) \longrightarrow T(A \otimes B)$$

satisfying certain relations [3]. In the case of a *strict* monoidal category, such as FüD, these amount to the requirement that  $\tau$  be a *morphism* of the monad structure. The corresponding laws are:

$$\mathrm{id}(A)\otimes \eta(B)\cdot \tau(A\ ,B)=\eta(A\otimes B):A\otimes B\longrightarrow T(A\otimes B)$$

and

 $id(A) \otimes \mu(B) \cdot \tau(A,B) = \tau(A,T(B)) \cdot T(\tau(A,B)) \cdot \mu(A \otimes B) : A \otimes T^2(B) \longrightarrow T(A \otimes B)$ 

In the case of the burrito monad, the strength,  $\tau$ , is the "wrapping in" transformation, which takes a "side" object A and a burrito T(B) and yields a burrito in which the side has been wrapped in to the burrito. This is most clearly illustrated by an example. Suppose that you begin with a bean burrito and a side of guacamole. By "wrapping in" the side, you may obtain a bean and guacamole burrito – which is clearly better. In this case, the monad strength laws require the following:

- strength unit law: If you first insert some beans into a simple burrito and next wrap-in a side of guac, the effect is the same as if you had inserted the guac and beans into a simple burrito together.
- strength multiplication law: If you have a compound bean burrito that you first merge into a simple one and you then wrap-in a side of guac, the effect is the same as if you had wrapped the guac into the outer, bean burrito, burrito, then wrapped the (now interstitial) guac into the inner, bean, burrito, and then finally merged the compound guac and bean burrito

into a simple one. This last equivalence is perhaps best understood as:

			guac and ((bean burrito) burrito)
	guac and ((bean burrito) burrito)	$\Rightarrow$	[wrap-in guac to outer burrito]
$\Rightarrow$	[merge compound burrito]		(guac and (bean burrito)) burrito
	guac and (bean burrito)	$\Rightarrow$	[wrap-in guac to inner burrito]
$\Rightarrow$	[wrap-in guac]		((guac and bean) burrito) burrito
	(guac and bean) burrito	$\Rightarrow$	[merge compound burrito]
			(guac and bean) burrito

1 (/1

. . . .

#### 5 **Functional Burritos**

Those coming to burritos from a functional programming background may prefer to understand them by way of the "return and bind" formulation of monads [8], popularized by the *typeclass* mechanism of languages such as Haskell.

From this perspective, the burrito monad's return is just the same as its unit  $\eta$ . Flipping argument order, we see that the **bind** operation,  $(A \rightarrow TB) \rightarrow$  $TA \rightarrow TB$ , transforms a burrito recipe into one that expects to receive its ingredients in burrito form. The monad laws in this formulation are satisfied just in case one takes flip bind f to be  $T(f) \cdot \mu(B)$ .

The T-image of the morphism f performs f while wrapped in a tortilla. Depending on the nature of the morphism, this may raise size issues. In the preceding discussion, we have assumed all burritos to be locally small.

#### 6 Conclusion and Related Work

As you can see, burritos are not so hard to understand, once viewed from the proper perspective - namely, that of abstract category theory. We hope that this little tutorial will encourage more researchers to incorporate burrito-theoretic results and methods into their own work.

Burrito-like sandwiches have emerged several times independently, but were not put on a solid theoretical footing until their connection to monads became apparent in the early 1970s [3, 7]. More recently, a connection to the Hegelian taco, a display of the 3-dimensional eight-element graphic monoid with five left ideals, has been worked out by Lawvere [4]. It is conjectured that weak equivalences exist to other wrap-like structures, but research in this area is presently ongoing.

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Paper 7: Burritos for the Hungry Mathematician

### A. G. Rating: 3 (weak accept) Confidence: 2/4

This paper presents a novel category theoretic understanding of burritos. This understanding is a major step forward in the eventual goal of understanding the categorical structure of  $F\ddot{u}d$ . The definition of the tortilla endofunctor is a significant research contribution that is a start at illuminating the mysterious structure of  $F\ddot{u}d$ . However, the reviewer is not satisfied with just the definition of the tortilla endofunctor and believes that either the author should define the other endofunctors in this category or prove a uniqueness theorem as to why the tortilla endofunctor is the only one possible. This reviewer suspects that there may actually be infinite endofunctors in  $F\ddot{u}d$  once one considers, crêpes, blini, wraps, etc – the whole set of circular two dimensional vessels for enclosing food.

### $Track \ Z$

## Computationalizing Computation

### 1. A New Paradigm for Certified Code Stefan Muller

Keywords: certified code, certified compiler, proof-carrying code

2. Beyond the Halting Problem: Higher Order Infinite Loop Checkers Jody Leonard and Aaron Santiago Keywords: computability, decidability, infinite, loop, checker

### 3. Bashing Haskell:

## Reimplementing the Parsec Library Inside the Unix Shell Mike Izbicki

Keywords: unix, sed, parsing, parsec, haskell, applicative, monad

### A New Paradigm for Certified Code

Stefan Muller

Carnegie Mellon University smuller@cs.cmu.edu

#### Abstract

Everyone likes running programs, but before you run a piece of code, you want to be sure that it's actually code. Utterly ignoring building on a large body of work in *certified code*, we solve this ever-so-common problem.

#### 1. Introduction

Dozens of prior studies over several years have worked in the area of "certified code" (e.g. [1–5, 7, 9, 10, 12–14]). Like all great researchers, the present author didn't read any of these papers, as such a literature study clouds one's mind with lesser ideas and stifles true innovation. Instead, this paper presents an entirely novel way of generating and running certified code. You're welcome.

In these fast-and-loose days of computing, it is common to assume that a given file is an executable binary, run chmod +x on it, and execute it willy-nilly. However, doing this on a non-executable file can severely damage one's computer<sup>1</sup>. It is thus vital to the security of computers that, prior to executing a file, we *certify* that it is, in fact, *code* (as opposed to, for example, a humorous animated GIF of a cat). This is the domain of *certified code*. In this paper, we describe CODECERT, a new, language-independent method of generating certified code from source, and running it safely.

#### 2. The CODECERT System

The key observation underlying CODECERT is that executable binaries are the result of running a compiler on a piece of source code. This observation, explained in Figure 1, means that, to certify that a file is a binary, and therefore code, we need only certify that it is the output of a compiler.

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Figure 1: A binary is the output of a compiler on source code. If the inputs are not a compiler and source code, no guarantees are possible.

<sup>&</sup>lt;sup>1</sup> Or gracefully throw an exception and exit, as the case may be.

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SIGBOVIK '15, April 1, 2015, Pittsburgh, Pennsylvania, USA



Figure 2: The CODECERT system compiles a given source file with a given compiler and compares the result with a given file. The file is a binary if and only if the results match.

Compilers	Not compilers
gcc	ls
javac	awk
ghc	echo
ocamlc	sleep
gc	apt-get
coqc	emacs
fbc	bash

Table 1: Comparison of compilers and non-compilers

The simplest way to do this is to keep as proof artifacts the source code and the compiler, and show that the purported binary is actually what is obtained by running the purported compiler on the purported source. This process is explained in further detail in Figure 2.

To produce certified code, the CODECERT system takes a purported binary, along with its source code and the compiler with which it was compiled. These three files are packaged together. When the certified binary is to be run, CODE-CERT compiles the packaged source code with the packaged compiler. If this matches the purported binary, the binary is executed. Otherwise, the file is determined to not be a binary, and the user is warned not to execute it.

#### 2.1 Certified Compilers

At this point, the astute reader may observe that the process described above works only if the compiler provided to CODECERT is actually a compiler. Otherwise, the "source code" could be, for example, an image and the "compiler" could be a program that, for example, adds captions to images. This concern led us to conduct novel research in the area of *certified compilers* [6, 8], related to certified code. Our method for certifying that a program is a compiler relies on a second key observation. This observation was reached after detailed study of a large number of compilers and noncompiler utilities, catalogued in Table 1. Note that all compilers in the list end in the letter "c" while no non-compilers do. The CODECERT code generator takes advantage of this fact to certify that the provided binary is a compiler before generating the package.

```
$ ocamlc -o hello hello.ml
$ ./mkcode ocamlc hello.ml hello hello_pkg
$ ./runcode hello_pkg
Hello, world!
$ ./mkcode ocamlc hello.ml cat.jpg hello_pkg
$ ./runcode hello_pkg
Code not certified!
```

Figure 3: In the first instance, CODECERT correctly determines that hello is code. In the second, it correctly determines that cat.jpg is not code.

#### 3. Proof of Correctness

We now formally prove that CODECERT is correct in that running a certified code package generated by CODECERT will proceed only if the provided file is indeed code.

**Theorem 1.** If CODECERT produces a certified code package from a file e, then either e is an executable or running the code package using CODECERT will produce an error.

*Proof.* By induction on the length of the filename of e. A zero-character filename is invalid, so the base case is trivial. If the length is n, rename e to a name of n - 1 characters. By induction, this new file, and therefore e, is either an executable or will produce an error.

#### 4. Implementation

Our CODECERT package consists of two utilities: mkcode and runcode. The mkcode utility takes as command-line arguments a source code file, its compiler, the name of the uncertified binary and the name of the certified package to output and, as the name suggests, mks a certified code package. This utility is 12 lines of Bash script code which certifies the compiler and, if valid, prepares a .tar archive of the provided files, along with the command line with which to invoke the compiler<sup>2</sup>.

The second utility, runcode, extracts the files from the archive, invokves the compiler and uses diff to compare the output with the provided binary. If they match, the binary is executed. Otherwise, an error is produced. This utility consists of nine lines of Bash code. Figure 3 shows two interactions with CODECERT.

#### 5. Related Work

A closely related avenue of research which we hope to soon explore (read: solve) is *proof-carrying code* [11]. For example, see Figure 4.

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<sup>&</sup>lt;sup>2</sup> This is assumed to be ./<compiler> -o <output> <src>. If the compiler arguments do not take this form, mkcode will fail gracefully and output an error. We assume. This hasn't actually been tested.

```
1 (* Suppose sqrt(2) = a/b where a, b are not both even.

2 * 2b'^2 = a'^2, so a'^2 is even, so a=2n

3 * 2b'^2 = 4n'^2

4 * b'^2 = 2n'^2

5 * b'^2 is even, so b is even. Contradiction.

6 *)

7

8 let rec fib n =

9 if n \le 1 then 1 else (fib (n - 1)) + (fib (n - 2))
```

Figure 4: This code carries a proof that  $\sqrt{2}$  is irrational. It also computes Fibonacci numbers.

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#### Beyond the Halting Problem Higher Order Infinite Loop Checkers

Jody Leonard and Aaron Santiago

jleonard110simons-rock.edu asantiago110simons-rock.edu Division of Science, Mathematics and Computing, Bard College at Simon's Rock

**Abstract.** The infamous *Halting Problem* asks whether it is possible to determine whether an arbitrary program P halts on arbitrary input x. It is well known that the Halting Problem is undecidable for all input pairs of P and x - however, this question nevertheless remains woefully unexplored. In this landmark paper, we reframe the investigation with a more practical construction: *infinite loop checkers*.

**Keywords:** computability, decidability, infinite, loop, checker.

#### 1 Introduction

In 1936, Alan Turing's delivered his paper "On Computable Numbers, with an Application to the Entscheidungsproblem" [3] as a response to the famous *Entscheidungsproblem*<sup>1</sup>. In essence, Turing showed that for all programs P and inputs to those programs x, the language

 $L_H \coloneqq \{(P, x) | P \text{ halts when run on } x\},\$ 

also known as the *Halting Problem*, is not computable on a Turing Machine. Since the Halting Problem can be reduced to the Entscheidungsproblem, it follows that the Entscheidungsproblem has no general solution.

Our paper does not challenge Turing's conclusions, but rather draws attention to some important concerns and limitations of Turing's circumstances:

• Before the 1990s, there was no sufficient method to test any of Turing's results because programming didn't exist yet. The release of Python and other programming languages have all but solved this problem.

- Technology now has reached levels of computational power that would be unfathomable to researchers of Turing's time. The clock speed of Turing Machines are lumps of dirt compared to the chips found in even the light switches of today.
- Alan Turing was a much too attractive man. This meant that his ability to design theoretically valid statements must have been impaired by his ability to socialize.

With these limitations in mind, it is important to reassess the foundations of Turing's arguments in order to continue computing as a whole. Even though no one can know for sure, the authors believe that without such a change in direction, computing will be forced to stop.

To this end, we re-define and operationalize the Halting Problem in terms of a construction we call the *infinite loop checker*. Critically, this construction allows us to better consider extrapolations of the Halting Problem, which we term *orders* of infinite loop checkers.

<sup>&</sup>lt;sup>1</sup> Elvish for "tree fecal issue". For more information, see [2].

#### 2 Definitions

We begin by establishing a key concept with Definition 1.

**Definition 1.** A program P verifies program S iff P returns True when its input is equivalent to S, and False otherwise.

We define an *infinite loop checker of or*der n to be a program that verifies a loop checker of order n-1. This allows a simple natural language definition given in Definition 2.

**Definition 2.** An infinite loop checker of order n is the following:

# "infinite loop $\underbrace{checker \dots checker}_{n \ times}$ "

For example, an infinite loop checker of order n = 420 is an infinite loop checker checker

checker checker. This is obviously a very high order. For convenience, particularly in dealing with high orders, we adopt the notation given in Definition 3.

**Definition 3.**  $ILC_n$  is an infinite loop checker of order n.

The above language-notated infinite loop checker is equivalent to  $\mathtt{ILC}_{420}.$ 

#### 3 The Infinite Loop Checker Checker

The Halting Problem, along with Turing's proof, is widely known. However, the definitions given in Section 2 prompt us to consider the case of  $ILC_2$ . Lemma 1 offers the first of our foundational results.

#### Lemma 1. $ILC_2$ is computable.

To prove Lemma 1, we provide pseudocode for what we believe to be a polytime algorithm. The approach is described in Algorithm 1.

Algorithm	1	Infinite	Loop	Checker
Checker				
Input: P, a p	orog	ram.		
Output: True	e if	P is an infi	inite loo	p checker;
False otherv	vise.			
return Fals	se			

A table containing the experimental runtimes of Algorithm 1 is given in Table  $1^2$ . From this table, we conclude that Algorithm 1 runs in O(1), because the *p*-values are good enough<sup>3</sup>. Further, it's clear that Algorithm 1 runs very quickly, as computing all of Table 1 took just under 70 units of time. A theoretical runtime analysis is pending construction of a program that can verify the runtime of Algorithm 1.

Table 1: Experimental Results of  $ILC_2$ 

Input (Description)	Output	Runtime
Bubblesort	False	6.902
Quicksort	False	6.900
Bogosort	False	6.899
Panicsort	False	6.901
blank file	False	6.898
Checker.tex	False	6.899
vista-sp2.iso <sup>4</sup>	False	6.897
hl3.exe	False	6.902
The Deep Web	False	6.903
$song.mp3^5$	False	6.899

#### 4 High Order Infinite Loop Checkers

In trying to aggressively improve the performance of our  $ILC_2$  implementations, we attempted to create a program to verify  $ILC_2$ , and found that, like  $ILC_1$ , this problem is also undecidable.

Lemma 2.  $ILC_3$  is not computable.

For a formal proof of Lemma 2, see the Halting Problem [3].

Further research revealed that increasing the order again led to another decidable problem, and that it has, in fact, an implementation identical to Algorithm 1.

Lemma 3.  $ILC_4$  is computable.

- <sup>3</sup> Confused readers are encouraged to consult Rumsey[1].
- <sup>4</sup> Acquired legally.
- <sup>5</sup> Available here: http://jabdownsmash.com/ sigbovik2015/song.mp3

<sup>&</sup>lt;sup>2</sup> Tests were performed on a 2010 Alienware M11x R2 running 32-bit Ubuntu through an emulated Commodore 64.

Lemmas 1, 2, and 3 lead us to consider Theorem 1.

**Theorem 1.** If n is of the form n = 2k, then  $ILC_n$  is decidable; if n is of the form n = 2k + 1, then  $ILC_n$  is undecidable.

To test Theorem 1, we created an arbitrary order infinite loop checker generator, and verified the first few trillion orders of infinite loop checkers. Pseudocode is given in Algorithm 2, and Table 2 outlines the fruits of our research up through  $ILC_{50}$ . So far, the results of this test have been consistent with Theorem 1. We leave the formal proof of Theorem 1 as an exercise to the reader<sup>6</sup>.

Algorithm 2 Infinite Loop Checker Gen-
erator
<b>Input:</b> <i>n</i> , a Natural number.
<b>Output:</b> $P$ , a program that is an implemen-
tation of $ILC_n$ ; False if not possible.
if $n$ is greater than 0 and even then
return "return False"
else
return False
end if

#### 5 Infinite Order Infinite Loop Checkers

Building on Definition 3, we can begin to approach the concept of high-order  $ILC_n$  programs theoretically. First, we observe a new approach to Definition 3 in Remark 1

Remark 1.  $ILC_n$  for  $n \ge 1$  is a program that verifies its input to be  $ILC_{n-1}$ .

To cover the case of  $ILC_1$ , we provide Definition 4.

**Definition 4.**  $ILC_0$  is an infinite loop.

<sup>&</sup>lt;sup>6</sup> Any completed exercises should be submitted to coders@simons-rock.edu for review.

шU	Oruer	Decideable:	numinine
$ILC_1$		False	N/A
$ILC_2$		True	O(1)
ILC <sub>3</sub>		False	N/Á
$ILC_4$		True	O(1)
$ILC_5$		False	N/Á
$ILC_6$		True	O(1)
ILC <sub>7</sub>		False	N/A
ILC <sub>8</sub>		True	O(1)
ILCo		False	N/A
ILC <sub>10</sub>		True	O(1)
ILC <sub>11</sub>		False	N/A
TLC12		True	O(1)
TLC <sub>12</sub>		False	N/A
TLC		True	O(1)
TI Cur		False	N/A
TIC.		True	O(1)
TI C		Falso	$N/\Delta$
TI C.		True	O(1)
TLC18		Falso	
TLC19		True	O(1)
TLC20		Falso	
		True	O(1)
TLC22		Falso	
TLC23		True	O(1)
TLC <sub>24</sub>		Falsa	
TLC25		Taise	O(1)
TLC26		Falca	
TLC <sub>27</sub>		Taise	O(1)
ILC <sub>28</sub>		True	
ILC <sub>29</sub>		False	N/A
ILC <sub>30</sub>		Irue Eslas	
ILC <sub>31</sub>		False	N/A
1LC <sub>32</sub>		True	
ILC <sub>33</sub>		False	N/A
ILC <sub>34</sub>		True	
ILC <sub>35</sub>		False	N/A
ILC <sub>36</sub>		Irue	
ILC <sub>37</sub>		False	N/A
ILC <sub>38</sub>		True	
ILC <sub>39</sub>		False	N/A
ILC <sub>40</sub>		True	O(1)
ILC <sub>41</sub>		False	N/A
ILC <sub>42</sub>		True	O(1)
ILC <sub>43</sub>		False	N/A
$ILC_{44}$		True	O(1)
ILC <sub>45</sub>		False	N/A
ILC <sub>46</sub>		True	O(1)
$ILC_{47}$		False	N/A

O(1)

N/A

O(1)

True

False

True

Table	2:I	nfinite	Loop	Checkers
ILC O		Deald	a a la la f	2 Durations

ILC<sub>48</sub>

ILC<sub>49</sub>

ILC<sub>50</sub>
Pseudocode for an implementation of  $ILC_0$  is provided in Algorithm 3, and is pending runtime analysis.

Algorithm 3 Infinite Loop
while True do
Nothing.
end while

Now consider  $\mathtt{ILC}_\infty.$  Remark 1 states that

 $ILC_{\infty} \ vertifies \ ILC_{\infty-1},$ 

but  $\infty - 1 = \infty$ , which implies that

 $ILC_{\infty} \ vertifies \ ILC_{\infty}$ 

or simply, that an *infinite order infinite loop checker* is a program that verifies itself. Pseudocode for an implementation of an infinite order infinite loop checker is provided in Algorithm 4.

Algorithm 4 Infinite Order Infinite Loop
Checker
Input: P a program.
<b>Output:</b> True if $P$ is equivalent to this pro-
gram; False otherwise.
Generate own source code $S$
if $P = S$ then
return True
else
return False
end if

### 6 Additional Results and Open Problems

Using the research techniques found in Sections 2, 3, and 4, we consider Definition 5 and suggest Lemmas 4 and 5 as a cursory exploration of the possibility of infinite order infinite loop checker checkers. We offer these Lemmas as open problems.

### Definition 5.

TOTICO	$verifies IOILCC_{n-1}$	if $n > 0$
IUILCCn	is $\mathtt{ILC}_\infty$	if $n = 0$

**Lemma 4.**  $IOILCC_1$  is not computable.

Lemma 5.  $IOILCC_2$  is computable.

The authors would like to explore the possibility of higher order infinite order infinite loop checker checkers themselves, however their machines are currently still stuck analyzing the runtime of the infinite loop algorithm, and it would seem that emulating C64 hardware on a five year old laptop is not granting them any favors.

Also, the possibility of exploring checkers in multiple dimensions might divulge more insight on the nature of Turing's original halting problem.



Fig. 1: A possible explanation of multidimensional infinite loop checkers.

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Paper 13: Beyond the Halting Problem

# Stefan Muller, Carnegie Mellon University Rating: $\infty$ (strong strong st

This is a very good paper. Allow me to explain my reasoning. Alan Turing's famous "On the Computable Numbers, with an Application to the Entscheidungsproblem" was a good paper, and this paper generalizes its findings to order  $\infty$ , which must make this paper  $\infty$  times better. As we all know,  $\infty \times \text{good} = \infty$ , so the goodness of this paper is  $\infty$ .

On the other hand, I was slightly confused by Section 6. Judging by Figure 1 (which was the only part of this section I read), this section discusses multi-dimensional infinite loop checkers, an amusing game played by homotopy theorists in which players must reduce their opponents' loops to points in an infinite, multi-dimensional non-Euclidean topological space. This is an excellent topic of study, but I don't see the relevance to the rest of the paper. Unless the authors have constructed an algorithm to verify programs which validate possible moves in multi-dimensional infinite loop checkers, since such a "multi-dimensional infinite loop checkers checker checker" would be a valuable contribution. In this latter case, the goodness of the paper is doubled to  $\infty$ , otherwise it is decreased slightly to  $\infty$  – confusing section =  $\infty$ .

One request I would make of the authors is to not further discuss the subject of Alan Turing with me until I finish reading his biography, as I'm only on Chapter 3 and don't want to be told how it ends. Judging by his healthy lifestyle and the importance of his scientific contributions, I can only assume he lived happily to a ripe old age and was revered by all as the King of Computers.

## Bashing Haskell: Reimplementing the Parsec Library Inside the Unix Shell

**Functional** Imperative Pearl

Mike Izbicki

University of California Riverside mike@izbicki.me

### Abstract

We introduce the Parsed suite of Unix command line tools. Parsed improves the classic sed program by incorporating ideas from the popular parsec Haskell library. In particular, the Unix pipe operator (|) corresponds exactly to the Applicative bind (\*>) in Haskell. The resulting syntax is both intuitive and powerful. The original syntax used by sed can match only regular languages; but our improved syntax can match any context sensitive language.

Keywords unix, sed, parsing, parsec, Haskell, applicative, monad

#### 1. Introduction

The stream editor (sed) is one of the oldest and most widely used Unix utilities. Unfortunately, it is a monolithic beast. It fails to live up to the Unix philosophy of "do one thing well." The problem is that sed tries to implement all regular expression features in a single executable. This ruins composibility. For example, let's say I have a simple sed command for deleting email addresses. Something like:

sed 's/[a-zA-Z0-9.]@[a-zA-Z0-9.]/xxx@xxx/g'

But in the file I'm working on, I only want to delete an email address if the line starts with the words CONFIDENTIAL. This should not be a hard task. We *should* be able to write another sed command for finding lines that begin with CONFIDENTIAL, then combine these two commands. But this is not possible using standard techniques. To solve our problem, we must rewrite an entirely new sed command from scratch. Within that command, we copy-and-paste our previously tested command:

```
sed 's/(CONFIDENTIAL.*)[a-zA-Z0-9.]@[a-zA-Z0-9.]/
$1xxx@xxx/q'
```

Real world experience suggests that this practice is a leading source of bugs for the modern sed programmer.<sup>1</sup> In this paper, we simplify shell based parsing by introducing techniques from functional programming into the Unix shell. Our Parsed library combines the best of sed with Haskell's excellent Parsec library.

Parsec is a simple Haskell library that makes parsing easy and fun. It provides a small set of simple higher order functions called combinators. By combining these combinators, we can create programs capable of parsing complex grammars. The Parsed library recreates these combinators within the Unix terminal. In particular, each combinator corresponds to either a shell script or shell function. We then combine these combinators using the standard Unix pipe. There are three combinators of particular importance: match, some, and choice. With these combinators, we can match any regular expression. But unlike sed, our combinators can take advantage of the shell's built-in expressivity to match any context sensitive language!

In the remainder of this paper, we give a brief tutorial on how to construct your own parsers using Parsed. We recommend that you install Parsed and follow along with our examples. Installing is easy. Just clone the git repo:

\$ git clone https://github.com/mikeizbicki/parsed

And add the resulting  ${\tt parsed/scripts}$  folder to your <code>PATH</code>:

\$ export PATH="\$(pwd)/parsed/scripts:\$PATH"

That's it! You're now ready to start parsing!

### 2. Matching strings

The most basic combinator is match. It's easiest to see how it works by example. Throughout this tutorial, we will first present the examples, and then their explanation.

\$ match hello <<< "goodbye"
\$ echo \$?</pre>

match takes a single command line argument, which is the string our parser is trying to match. In the above example, this is the string hello. The text to be parsed comes from stdin. In the above example, we use bash's built-in <<< syntax, which redirects the contents of the following string (goodbye) to stdin. The exit code of the previously run program is stored in the shell variable \$?. In the above example, our parser failed (the string hello does not match the string goodbye), so \$? contains a non-zero value.

Now let's see what a successful parse looks like:

```
$ match hello <<< "hello"
hello
$ echo $?
0
```

When match succeeds, the matched text gets printed to stderr. This is where the output string hello comes from in the above example. Since parsing succeeded, match returned an exit code of 0. As you can see, match is a very simple parser. It is normally combined with other parsers.

### **3.** Combining parsers

We combine parsers using the standard unix pipe (|). For example, let's create a parser that first matches the string hello and then matches the string world:

```
$ (match hello | match world) <<< "helloworld"
helloworld
$ echo $?</pre>
```

0

<sup>&</sup>lt;sup>1</sup> Can you spot the bug in the command?

#### Script 1 match

#### #!/bin/sh

```
# check for the correct number of arguments
if [ -z "$1" ] || [ ! -z "$2" ]; then
    echo "match_requires_exactly_one_argument"
    exit 255
fi
# When reading from stdin, the shell ignores the
    contents of the IFS variable. By default,
    this is set to whitespace. In order to be
    able to read whitespace, we must set IFS to
    nothing.
IFS=''
# read in exactly as some characters as are in
    the first command line argument
read -rn "${#1}" in
# if we parse correctly
if [ "$1" = "$in" ]; then
    # print the parsed string to stderr
echo -n "$in" 1>&2
    # forward the unparsed contents of stdin
    cat
    # signal that parsing succeeded
    exit 0
else
    # parsing failed
    exit 1
fi
```

Parsing succeeds for both calls to match, so parsing succeeds overall. To see how piping combines parsers, we need to take a more careful look at the match script. Like all combinators in the Parsed library, match is written in POSIX compliant shell. The full source code is shown in Script 1 above.

We've already seen that when match succeeds, the matched string is printed to stderr; but additionally, any unparsed text is printed to stdout. This is demonstrated by the following two tests:

```
$ match hello <<< "helloworld" 1> /dev/null
hello
$ match hello <<< "helloworld" 2> /dev/null
world
```

As a reminder, by putting a number in front of the output redirection operator >, we redirect the contents of that file descriptor to the specified file. File descriptor 1 corresponds to stdout and 2 to stderr. So the first command above discards stdout; it shows only the text that was successfully parsed. The second command above discards stderr; it shows only the text that is sent to any subsequent parsers.

It is possible for the first parser to succeed and the second to fail. In this case, the succeeding parsers still print their output to stderr, but parsing fails overall:

```
$ (match hello | match world) <<< "hellogoodbye"
hello
$ echo $?
1</pre>
```

Concatenating two match parsers is relatively uninteresting. We could have just concatenated the arguments to match! So now let's introduce a new combinator called eof which matches the end of file. That is, eof will succeed only if the stdin buffer has been

### $Script \ 2 \ \texttt{eof}$

#### #!/bin/sh

```
# Try to read a single character into the
    variable $next. If next is empty, we're at
    the end of file, so parsing succeeds.
IFS=
read -n 1 next
if [ -z $next ]; then exit 0; else exit 1; fi
```

closed because there is no more input to parse. The source code for eof is much simpler than for match, and is shown in Script 2.

These next two examples demonstrate the effect of the eof combinator. First, we try matching the string hello on the input hellohello:

```
$ match hello <<< "hellohello"
hellohello
$ echo $?
0
```

Parsing succeeds; we print the contents of the parsed text (hello) to stderr; and we print the remaining content to be parsed (hello) to stdout. If, however, we apply the eof combinator:

```
$ (match hello | eof) <<< "hellohello"
hello
$ echo $?
1</pre>
```

Parsing now fails because the input was too long. Shortening the input again causes parsing to succeed:

\$ (match hello | eof) <<< "hello"
hello
\$ echo \$?</pre>

Now that we know how to combine two simple parsers, we're ready for some more complex parsers.

### 4. Iterating some parsers

The some combinator lets us apply a parser zero or more times. some corresponds to the Kleene star  $(\star)$  operator used in sed and most other regular expression tools. some takes a single command line argument, which is the parser we will be applying zero or more times. For example:

```
$ (some "match_hello" | eof) <<< "hellohello"
hellohello
$ echo $?
0
```

The above example succeeds because the some "match hello" parser consumes *both* occurrences of hello. As already mentioned, some need not consume any input:

```
$ some "match_hello" <<< ""
$ echo $?
0
$ some "match_hello" <<< "goodbye"
$ echo $?
0
</pre>
```

In fact, the some used by itself can never fail—it will always just parse the empty string. In order to force failures, we must concatenate some with another parser like so:

```
$ (some "match_hello" | eof) <<< "goodbye"
$ echo $?
1</pre>
```

Script 3 some

#!/bin/sh

```
# check for the correct number of arguments
if [ -z "$1" ] || [ ! -z "$2" ]; then
    echo "many_requires_exactly_one_argument"
    exit 255
fi
# put the contents of stdin into a variable so we
     can check if it's empty
stdin=$(cat)
# if we still have input and parsing succeeded
if [ ! -z "$stdin" ] && stdout='eval "$1" <<< "
    $stdin"`; then
    # run this parser again
    "$0" "$1" <<< "$stdout"
else
    # stop running this parser
    cat <<< "$stdin"
fi
```

Unfortunately, the some combinator breaks the ability to use POSIX pipes for concatenation as we did above. Consider this example:

```
$ (match hello | some "match_hello") <<< ""</pre>
$
 echo $?
```

Our first match parser failed because there was no input. Then we call the some parser. There is still no input, so some succeeds. Since some was the last command to execute, \$? contains its exit code which is 0.

The problem is that the standard POSIX \$? variable has the wrong behavior. We need a variable that will report if any of the commands in the pipe chain failed. There is no POSIX compliant way to do this. But more modern shells like bash offer a simple fix. The command

```
$ set -o pipefail
```

modifies the semantics of the \$? variable so that it contains zero only if all commands in the pipe chain succeed; otherwise, it contains the exit code of the first process to exit with non-zero status. This command need only be run once per bash session. Thereafter, we can rerun the incorrect example above to get the correct output:

```
$ (match hello | some "match_hello") <<< ""</pre>
$
 echo $?
```

The code for the some combinator is shown in Script 3 above.

#### 5. Custom combinatorial explosion

Most regular expression libraries offer a primitive combinator + that matches one or more occurrences of a previous parser. Parsed does not have such a primitive operator because it is easy to build it using only the | and some combinators. We call the resulting operator many, and we implement it by creating a bash function:

```
$ many() { $1 | some "$1"; }
```

Recall that the \$1 variable will contain the first parameter to the many function. In this case, that parameter must be a parser. We Script 4 many

```
#!/bin/bash
set -o pipefail
$1 | some "$1"
exit $?
```

can use our new combinator to simplify the examples from the previous section:

```
$ many "match_hello" <<< ""
$ echo $?
$ many "match_hello" <<< "hello"
hello
$ echo $?
```

Unfortunately, Bash functions do not last between sessions. If we want something more permanent, we can create a script file instead. In fact, the many combinator is so useful that it comes built-in to the Parsed library. You can find its source code in Script 4 above. When the script file starts, it will not inherit the settings of its parent process in the same way that our many function did. Therefore, we must specifically re-setup our non-POSIX pipes at the beginning of every script that uses them.

#### The program of choice 6.

The last combintor we need for parsing regular languages is called choice. The match and many combinators required exactly one input, but choice takes an arbitrary number of input parameters. Each parameter is a parser. For each of these parsers, choice applies it to stdin. If it succeeds, then choice returns success. If it fails, then choice goes on to the next parameter. If all parsers fail, then choice fails as well.

Here's a simple example using just the match combinator:

```
$ choice "match_hello" "match_hola" <<< hello</pre>
hello
$ echo $?
$ choice "match_hello" "match_hola" <<< hola
hola
$ echo $?
$ choice "match_hello" "match_hola" <<< goodbye</pre>
  echo $?
```

Our parser succeeds when the input was either hello or hola, but fails on any other input.

#### 7. Free your context

0

\$

1

In the intro we claimed that Parsed is strictly more powerful than sed. We now demonstrate this point by parsing a context free language. Sed only supports regular expressions. The reason Parsed has this extra power is because we can define our own recursive parsers using standard shell syntax.

To demonstrate this capability, we will write a parser that checks for balanaced parenthesis. First, let's define a small combinator paren that takes a single parser as an argument and creates a parser that succeeds only when the parameter is surrounded by parentheses:

```
$ paren() { match "(" | $1 | match ")"; }
```

And let's test it:

### Script 5 choice

#### #!/bin/bash

```
# We need to store the contents of stdin
    explicitly to a file. When we call one of our candidate parsers, it will consume some
    of the input form stdin. We need to restore
    that input before calling the next parser.
stdin=$(tempfile)
cat >"$stdin"
# If stdin is empty, then we're done with
    recursion; parsing succeeded
if [ ! -s "$stdin" ]; then
    exit 0
fi
# For similar reasons, we'll need to store the
    output of our parsers.
stdout=$(tempfile)
stderr=$(tempfile)
# For each parser passed in as a command line arg
for cmd in "$@"; do
    # Run the parser; if it succeeds, then pass
    on its results
    if $(eval "$cmd" <"$stdin" 1>"$stdout" 2>"
    $stderr") ; then
        cat "$stderr" >&2
         cat "$stdout"
         exit 0
    fi
done
# All parsers failed, so we failed
exit 1
```

```
$ paren "match_hello" <<< "hello"
$ echo $?
1
$ paren "match_hello" <<< "(hello)"
(hello)
$ echo $?</pre>
```

We will use paren to write a combinator maybeparen that accepts whether or not the parameter parser is surrounded by parenthesis. Here is a reasonable first attempt:

\$ maybeparen() { choice "\$1" "paren\_\$1"; }

Unfortunately, this doesn't work due to scoping issues with bash. When we run our command, we get an error:

```
$ maybeparen "match_a" <<< "(a)"
choice: line 7: paren: command not found</pre>
```

We get this error because the choice combinator is its own shell script. When this script gets executed, a new shell process starts with a clean set of environment variables. In the context of this subprocess, the paren function we created above doesn't exist.

There are two ways to solve this problem. The simplest is to use the following bash-specific syntax:

```
$ export -f paren
```

This command tells the running bash shell that any subshells it spawns should also have access to the paren function. Now when we try running our previous tests: Script 6 parens

```
#!/bin/bash
choice "$1" "match_'('_|_par_\"$1\"_|_match_')'"

$ maybeparen "match_a" <<< "a"
a
$ echo $?</pre>
```

```
0
$ maybeparen "match_a" <<< "(a)"
$ echo $?
```

We still get a parse error! What's happening is that we actually defined the maybeparen function incorrectly. Here is the correct definition:

\$ maybeparen() { choice "\$1" "paren\_\"\$1\""; }

The only difference is that the correct definition surrounds our \$1 parameter with quotation marks. This ensures that the entire value of the variable gets passed as a single parameter to the paren combinator. Because these quotation marks are within quotation marks, they must be escaped with backslashes. Arrgh!

We are now ready to define a combinator parens that matches any number of balanced parentheses. In order to avoid the need for a set of triply nested quotation marks, we will put the parens combinator within a script file (instead of a function) and we will manually inline our call to the paren combinator. Script 6 above contains the final result. And now let's test our creation:

```
$ par "match_a" <<< "(((a)))"
(((a)))
$ echo $?
0
$ par "match_a" <<< "(((b)))"
$ echo $?
1
$ par "match_a" <<< "(((a"
$ echo $?
1
</pre>
```

We've successfully parsed a context free language :)

#### 8. Discussion

This is only a very brief introduction to the capabilities of our Parsed library. Additional under-documented features include: (1) We can use shell variables to simulate Haskell's Monad type class. In particular, the shell code:

var=\$(func)

is equivalent to the haskell do-notation code:

var <- func

In fact, all shell commands can be thought of as being within the IO monad wrapped within the ParsecT transformer. This leads us to our next under-documented feature. (2) Arbitrary commands can be used in parsers. Want to punish your users when they make syntax errors? Just add an rm  $-rf \star$  at the appropriate place in your combinators.

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[1] Daan Leijen and Erik Meijer. Parsec: Direct style monadic parser combinators for the real world. 2002.

## Track W

# Last Period Honors English Class

## 1. Programming Language Fan Fiction Stefan Muller

Keywords: type languages, programming fiction, fan theory

## 2. Acronymy: A Bidirectional Dictionary David Renshaw Keywords: knowingly, elevate, your, writing, on, relevant, directed, searches

3. Another Article that Makes Bibliometric Analysis a Bit Harder J. Pfeffer and J. Pfeffer Keywords: bibliometrics, j. pfeffer, j pfeffer

## 4. Comment: SIGBOVIK Should Ban Conclusions Jim McCann

Keywords: basp, hasp, grasp, tasp, masp, lasp, dasp

## 5. The Portmantout

Dr. Tom Murphy VII Ph.D.\* Keywords: last-minute treats, lexical feats, brogrammar

## Programming Language Fan Fiction (extended abstract)

Stefan Muller, Carnegie Mellon University

Programming language theory and design is an area of research in which authors frequently make design decisions. For example, authors might choose between call-by-name and call-by value; simply typed, dependently typed and untyped; intensional and extensional; predicative and impredicative; C-style syntax and ML-style syntax; statically and dynamically typed; garbage-collected and useless, etc. Inevitably, readers of these papers wonder what would happen if one of these design decisions were made differently. This is not a feature unique to programming languages; *fan fiction* is a popular process in which devotees of a work of fiction reimagine the work in their own way. It thus seems that programming languages and fan fiction could be combined to form a large body of new ideas, and it is the author's opinion that SIGBOVIK is a fine venue for such ideas.

Here, we present a number of avenues for development of programming language fan fiction. Some of these areas appear novel; in others, some work has already been done which can now be drawn under the umbrella of programming language fan fiction.

- Alternate notions of type membership. Type theories typically define the *canonical forms* of a particular type, but occasionally variations on this canon are possible. For example, in a strict language, canonical forms of pair type are  $(v_1, v_2)$  where  $v_1$  and  $v_2$  are themselves irreducible. Proponents of laziness might instead consider values of pair type to be  $(e_1, e_2)$  where  $e_1$  and  $e_2$  are arbitrary expressions. Expressions of a type which are considered by fans of a type theory, but not by the original presentation, to be irreducible are known as *headcanonical forms* or, if accepted by a large fanbase, *fanonical forms*.<sup>1</sup>
- Hacking new features into old languages. A common source of complaints about programming languages comes from the fact that a particular feature isn't present in a particular language. This complaint generally takes the form "I'd consider using (language) if only it had (feature)!" Examples include:
  - Statically-typed Python<sup>2</sup>
  - Garbage-collected C [1]
  - Concurrent ML [2]
  - LaTeX with types
  - LaTeX with decent syntax
  - LaTeX with any features at all

Some of the above are considered *conservative extensions*. Often, however, adding a particular feature to a particular language breaks a desired soundness property, makes type checking undecidable or causes various other havoc. This is generally not considered a problem in fan fiction, so have at it.

• Meta-properties of fan fiction. One interesting area of future research is the application of programming language techniques to the study of fan fiction. For example, fan fiction can be "Kripked" (a reference to author Eric Kripke) if it is validated by new canon. However, this assumes that the development of canon is linear. Often in computer science research, however, new developments will build

<sup>&</sup>lt;sup>1</sup>Note that this terminology is itself subject to debate. Confusingly, some authors of type theory fan fiction believe that the latter forms should be known as *headcanonical forms* and the former should be *weak headcanonical forms*.

 $<sup>^{2}</sup> https://github.com/illume/static_checking_python$ 

off of older ones in a nonlinear, branching fashion. This leads to the question of whether programming language fan fiction can be "Kripked" (a reference to logician Saul Kripke) in a way consistent with nonlinear reachability graphs.

• Fan fiction of type theory itself. Fans can make fan fiction not just of particular programming languages or type theories, but of the subject of type theory itself. In important prior work in this area, languages have been developed which are clearly based upon fan fiction-style manipulations of type theory itself<sup>3</sup>.

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<sup>&</sup>lt;sup>3</sup>https://www.haskell.org



Paper 16: Programming Language Fan Fiction (extended abstract)

## xOXoPHP\_pr0graming\_luvaaaa\_1997oXOx Rating: \*\*\* Confidence: oh yea baby ;)

Kyaaaaaa!  $(^{o}\nabla^{o})/$  SOOOOOOO happy to C some proper luv for fan fiction! especially since im learning how to program rite now, this is wayyy interesting~~~

I was really disapointed tho to see the author didn't ship his "types" w/ my fav paper from 2013, "Fandomized Algorithms and Fandom Number Generation"  $\mathbf{\sigma}_{-}\mathbf{\sigma}$  its my OTP!!!

### Acronymy: A Bidirectional Dictionary

https://dwrensha.ws/acronymy

### David Renshaw

Dictionaries are useful language reference guides that associate words with meanings, but in their traditional form they only solve half of the problem. They can map a given word to a definition, but they do not work in the opposite direction. What if you know a word's definition, but can't remember the word itself? Acronymy is a new dictionary for American English that aims to remedy this situation. Every definition in Acronymy can be efficiently and robustly mapped back to the word it defines. Even if you only remember *part* of a definition, it will help you remember the word! The trick is that Acronymy defines every word as an *acronym*. That is, the initial letters of the definition spell out the defined word. For example, "scallop" might be defined as "results are not deterministic or meditated." Acronymy is not yet complete, however. It needs your help! You can browse its current state and contribute new definitions by visiting https://dwrensha.ws/acronymy.

# Another article that makes bibliometric analysis a bit harder

J. Pfeffer J. Pfeffer Carnegie Mellon University Stanford University

April 1, 2015

There are many authors publishing many articles in a wide variety of scientific fields. Some of these researchers analyze the collaboration among researchers by looking at copublishing or citation behavior. "A key challenge when working with publication data is to disambiguate different authors carrying the same name, as accidentally merging multiple authors can distort results massively. This challenge is even harder when an initial is used in place of a first name. The goal of this article is to exacerbate this challenge and to make bibliometric analysis harder still.

### 1 Introduction

Researchers publish a lot, on many topics. They publish about people (J. Pfeffer, 1998; al. et J. Pfeffer, 1978; J. Pfeffer, 1994), organizations (J. Pfeffer et al., 2003; J. Pfeffer, 1992; J. Pfeffer et al., 1981), networks (J. Pfeffer et al., 2012; al. et J. Pfeffer, 2012; J. Pfeffer et al., 2011), time lords (al. et J. Pfeffer, 2013), as well as far more complicated topics (al. et J. Pfeffer, 1986; al. et J. Pfeffer et al., 1997). More recently, researchers are more and more interested in social media stuff (al. et J. Pfeffer, 2014; J. Pfeffer et al., 2014; al. et J. Pfeffer, 2014; al. et J. Pfeffer et al., 2013; J. Pfeffer et al., 2013; J. Pfeffer et al., 2014; al. et J. Pfeffer et al., 2013; J. Pfeffer et al., 2014; al. et J. Pfeffer et al., 2014; al. et J. Pfeffer et al., 2013; J. Pfeffer et al., 2014; al. et J. Pfeffer et al., 2013; J. Pfeffer et al., 2014; al. et J. Pfeffer et al., 2014; J. Pfeffer et al., 2014; al. et J. Pfeffer et al.



Figure 1: Research products by year for "J Pfeffer" on Google Scholar. There are an additional 1,660 results from year 0 to year 1989, resulting cumulatively in about 10,850 research products.

Intriguingly, publishing a lot is neither a new nor a completed phenomenon. As a matter of fact, *J. Pfeffer* (as well as others) has been creating more and more research products every year (see Figure 1). However, recursive citations can be seen as contemporary activity (J. Pfeffer & J. Pfeffer, 2015).

The contributions of our work are:

- We show that co-publishing analysis can be quite hard;
- We make co-publishing analysis even harder;
- By adding some random *J. Pfeffer* references to our paper, we create very interesting artifacts for future co-citation analysis.

### 2 Some Analysis

In order to show a network visualization and a ranking, we extracted the first 1,000 results from a Google Scholar search with "J. Pfeffer" and constructed a network (al. et J. Pfeffer, 2012). Nodes in this network represent people, i.e. J. Pfeffer and others. Links connect these nodes in case of at least one shared publication. The result can be seen in Figure 2(a). Authors that share multiple publications are connected by a thicker line.

To quantify the importance of J. Pfeffer in this network, we calculated betweenness centrality and present the very obvious results in Figure 2(b).

## 3 Outlook

To assess the importance of this issue for bibliometric analyses of the years to come, we estimate future levels of activity based on the previous scientific productivity of *J. Pfeffer*. Using data from



(a) Impressive Collaboration Network

(b) Intimidating Ranking

Figure 2: The pretty impressive collaboration network of *J. Pfeffer*, based on top 1,000 results of a Google Scholar search as well as betweenness centrality ranking in this network. Out of respect to the co-authors of *J. Pfeffer*, we keep quiet about their identities.



Figure 3: Estimated future productivity of "J Pfeffer" by year based on exponential growth fitted on historic data.

Figure 1, we first fit an exponential function to describe historic activity. It is important to notice that the following exponential function almost perfectly  $(R^2 = 0.9471)$  describes our historic data:

 $y = 88.43e^{0.0919*(year - 1989)}$ 

Figure 3 shows the full extend of the *J. Pfeffer* problem. Assuming a continued exponential growth, we expect about 270,000 cumulative research products by the year 2050.

### 4 Conclusions

It is okay to have a common family name and to give your child a boring first name. However, please consider one or more middle names to give her or him a head start in terms of an unmistakable identity. Exemplary behavior was shown by the parents of J.M. Pfeffer (J.M. Pfeffer et al., 2012; J.M. Pfeffer et al., 2013) and J.T. Pfeffer (J.T. Pfeffer, 1974; J.T. Pfeffer, 1992). In countries in which ~100 million people share the same family name, we recommend five middle names with at least two being picked completely at random.

## **5** Acknowledgments

The authors will always be grateful to Google Scholar for indexing this article. Without their greedy literature gathering approach, our work would be preposterous.

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## **Comment: SIGBOVIK Should Ban Conclusions**

### Jim McCann\* TCHOW llc

It has recently come to my attention that some elements of the scientific community, distressed by the mis-use of inferential statistics to support weak results in their fields, have taken drastic measures. Particularly bold has been the editorial board of the BASP journal, which have decided to *ban p*-values altogether<sup>†</sup>.

In fact, any and all types of inferential statistics – including confidence intervals and F-values – may no longer be included in BASP publications.

In other words, from this point forward, BASP papers will only be allowed to include results that "kind of look significant", but haven't been vetted by any statistical processes.<sup>‡</sup> I imagine this will also include studies where the cohorts "are not quite the same if you sort of look at this graph, I guess."

This is a bold stance, and I think we, as ACH members, would be remiss if we were to take a stance any less bold. Which is why I propose that SIGBOVIK – from this day forward – *should ban conclusions*.

Just as the BASP editorial board has so rightly observed that *p*-values can be flawed by mis-application of statistical mathematics, so too can conclusions be flawed by the mis-application of reasoning. In recognition of this, starting in 2016, I strongly suggest that any papers under review for SIGBOVIK (or other ACH conferences) that contain conclusions, arguments, logic, reasoning, or results be summarily rejected.

Of course, even this provision may not be sufficient, since readers may draw their own conclusions from any suggestions, statements, or data presented by authors. Thus, I suggest a phased plan to remove any potential of readers being mislead, with increasing strictures over the subsequent four years to allow authors to adapt their style (and to shovel any unpublished old results out while the shovelling is good).

### Plan:

2016 Conclusions banned.

- **2017** SIGBOVIK papers should no longer be allowed to contain data, since errors in data measurement might lead to improper conclusions on the part of the reader. (Though, thankfully, not on the part of the author, owning to 2016's ban.)
- **2018** The editorial board of SIGBOVIK should additionally summarily reject any papers that contain words other than in the title. Words are the primary component of lies, and the goal of science is truth, not lies. I, for one, welcome a more figure-driven publication style.
- **2019** In the following year, titles will also be banned. Papers will consist of wordless pictures, possibly graphs. (Which should have the added benefit of stimulating research into indexing and search on a wordless corpus.)
- **2020** Finally, in 2020, the ACH can take the ultimate step of banning all papers from SIGBOVIK, creating the world's second fully-correct journal. This will be an exciting time for science.

Fellow ACH members, I hope you will join me in urging the editorial board of SIGBOVIK to enact this plan. While it may seem drastic, it is the only way for the SIGBOVIK community to continue hold itself to the high standards of quality for which is has become known.

Yours,

James McCann, Ph.D.

<sup>\*</sup>e-mail: ix@tchow.com

<sup>&</sup>lt;sup>†</sup>http://www.nature.com/news/psychology-journal-bans-p-values-1.17001

<sup>&</sup>lt;sup>‡</sup>Technically, Beysian statistics are allowable on a case-by-case basis, though prior evidence suggests that they are unlikely to see the light of day.



Paper 15: Comment: SIGBOVIK Should Ban Conclusions

I. Ohnli-Skymmdit Rating: 2 (weak reject) Confidence: 2/4

This paper argues that conclusions are a misapplication of statistical mathematics, and therefore should be required in future years of BASP.

The author did not summarize his points at the end of the paper, so I had a hard time following the argument. The timeline in the right column would have been easier to read if it used fewer words.

## The Portmantout

### Dr. Tom Murphy VII Ph.D.\*

1 April 2015

### 1 Introduction

A *portmanteau*, henceforewith non-italicized, is a stringin'-together of two words to make a new word, like "brogrammer" (brother + programmer; a programmer who is your brother), "hupset" (hungry + upset; a bit more passive than hangry), or "webinar" (web + nerd). Portmanteaus were invented by Lewis Carroll, the Jabberwock of wordplay.

It is natural to think of generalizations of the portmanteau, such as the *portmantrois*,<sup>1</sup> (itself a portmanteau of **portmanteau** + trois, French-language for three) the human-centipedification of *three* words, such as "anachillaxis" (anaphylaxis + chill + relax; a severe allergic reaction to idleness) or "brogrammermaid" (brother + programmer + mermaid; a programmer who is your brother and a mermaid).

In this paper I present the world's first  $(?)^{23}$  portmantout, a portmanteau of all English-language words (tout means "all" in French-language). I also considered calling this a portmantotal, portmantotale, etc., as well as portmantoutal (a portmantroix of the first three) or even portmantoutale. You kind of see how this can get out of hand. The word is 630,408 letters long and contains all 108,709 words in a particular wordlist called wordlist.asc.<sup>4</sup> Even though nobody can really agree what all the words in English are, the technique used to generate this portmantout should work for most very long word lists, although we will see in Section 3.2 that a handful of words are very important.

Since the word itself is 11 pages long in 4pt type with .75 linespacing, and this SIGBOVIK proceedings is positively overfull hbox with content, we should probably get on with it.

## 2 Computationalizing "portmanteau"

A real portmanteau is usually phonetic, like "portmantotally" is about the sound of "—teau" being the same as "to—". It's also not unusual for part of the word to be completely dropped, as in "chillax", which drops the "re—" from relax. They are also usually clever or meaningful. For the sake of computing a portmantout, we need to make some rules about what it is, and it can't require cleverness or semantic/phonemic interpretation of words if I'm going to start and complete this project on the day of the SIGBOVIK deadline.

Generalized portmanteau. For a set of strings L, a string s is a generalized portmanteau if the entire string can be covered by strings in L. A cover is a set of word occurrences  $W = \langle m, n \rangle$ , where  $s_m - s_n$  (the substring starting at offset m and ending at n, inclusive) is in L, and, taken sorted by the m component,  $W_{i,n} >= W_{i+1} \cdot m$  for each i in range. For example,

## temper red rewrotempered rewrote

This string can be covered by rewrote, temper, and red, so it is a generalized portmanteau if these three strings are in L. (Spoiler alert: L is English-language, so they are.) Importantly, the covering strings overlap: rewro, temper and ed on their own would not cover this string (and rewro is not a word). Therefore, we cannot simply concatenate the entire dictionary.

**Portmantout.** A generalized portmanteau is a portmantout if it contains every string in L as a substring. The words need not be in its cover, as there may be muliple covers (In fact I conspicuously did not choose the simpler one rewrote + tempered.) Other words, like wrote, rote and rot are in there too "for free", even though they may not be able to participate in a legal cover.

A word may appear multiple times; we just have to get them all. This is fairly unavoidable—the word a appears 60,374 times in the portmantout. Perhaps more surprising is that the word iraq appears 315 times.

<sup>\*</sup>Copyright © 2015 the Regents of the Wikiplia Foundation. Appears in SIGBOVIK 2015 with the **etaoin shrdlu** of the Association for Computational Heresy; *IEEEEEE!* press, Verlag-Verlag volume no. 0x40-2A. BTC 0.00

<sup>&</sup>lt;sup>1</sup>Graham Smith, personal communication.

 $<sup>^{2}</sup>$ I did a couple Google searches; seems good enough.

<sup>&</sup>lt;sup>3</sup>Enjoy source code: http://sourceforge.net/p/tom7misc/svn/HEAD/tree/trunk/portmantout

<sup>&</sup>lt;sup>4</sup>Tom Murphy VII, "What words ought to exist?", SIGBOVIK 2011

Note that a "generalized" portmanteau does not actually include most colloquial portmanteaus; brogrammer cannot be covered since we dropped the "p—" in programmer. brogrammar is also not a generalized portmanteau since bro and grammar do not overlap, yo, but I think it would be accepted colloquially by most dudes. Disrupt!

## 3 Generating a portmantout

It's fairly straightforward handwaving to see that generating the shortest portmantout is NP-complete. Seeing that it is in NP is easy; we just need to check the cover and look up all the substrings, which is clearly polynomial. It is probably NP-hard because the traveling salesman problem can be reduced to it; for each node in the graph, generate a two-symbol word xy where x and y are fresh symbols; for each edge between cities  $x_iy_i$  and  $x_jy_j$  generate a string  $y_iu^wx_j$ , where u is also a fresh symbol repeated w times, the cost of the edge. This allows us only to join two city words by using a corresponding edge word.<sup>5</sup>

OK but good news! Since it's NP-complete, we know that we can come up with a solution that's both non-optimal and slow, and we can still feel pretty good about it. We proceed in two steps: Generating particles eagerly, and then joining them together.

### 3.1 Generating particles

For the first step, we load up all the words, and insert each word into a multimap, keyed by each of its non-empty prefixes. We then start by initializing a particle from any word; we choose **portmanteau** to start, obviously. Then, repeatedly:

- Check each suffix of the particle in descending length-order,
  - If we have a word that has not already been used, strip the suffix from its start and append the remainder to the particle
- Otherwise, emit the particle and start a new one with any unused word.

As an additional optimization, we discard words that are substrings of any particle. This search makes the program much slower, but it produces a much more efficient portmantout.

This always makes progress, using up one word at each step: We either append it to our current particle, or we start a new particle with a word. The particles are all generalized portmanteaus by construction, because each added word has non-empty overlap with the previous one. Here's an example particle: overmagnifyingearlesshrimpierabbinicalcicadaeratorshrimpiestandardizableaseholdershrimpingementshrimpsychedelically (overmagnifying + gearless + shrimpier + rabbinical + calc + cicada + aerators + shrimpiest + standardizable + leaseholders + shrimping + impingements + shrimps + psychedelically; presumably having something to do with shrimp).

At this point, we have about 38,000 particles, many of which are a single word. English contains many imbalances, like vastly more words ending with "-y" (10,071) than beginning "y-" (only 338), so it is not hard to see how we may get stuck with no new words to add to a particle. We've also used each word only once, and locally maximized the amount of overlap. If we can join these particles together in a valid way, we'll have a portmantout.

### 3.2 Joining particles

Since we've already used every word, and, by construction, these particles cannot be adjoined directly, we know we will need to reuse some words to join them together. A simple way to do this is to construct a table of size  $26^2$  that for every pair of letters *a* and *b*, contains a short word that starts with *a* and ends with *b*. 86% of the table entries can be filled in, but some letters are very tricky: For example, almost no words end with "q" (we have only colloq and iraq in our dictionary), and there are no words that start with "v" and end with "f". Fortunately, if we consider all two-word (generalized) portmanteaus, using basically the same algorithm as in Section 3.1, we can fill the table completely (Figure 1).

It is lucky for the existence of words like iraq; they are used for many of the entries in the "q" column. In fact, without a handful of such words, it might be the case that English would not permit a portmantotal! There are probably some less irregular languages that cannot achieve this lexical feat. :'-(

This table alone would allow us a very simple algorithm for generating a valid portmantotal: Just take words from the dictionary and concatenate them, but when putting e.g. tv and farm together, we use the v-f linker vetof (veto + of) from the table. We can't ever fail! However, this would produce a portmantout that's bigger than the dictionary itself, which isn't very economical. Rather than use the whole dictionary this way, we instead join all of the 38,000 particles from the previous section. These are much more compact. And now we are done!

### 4 The portmantout

This portmantout is 630,408 letters long; there are 931,823 total letters in the dictionary so this is a compression ratio of 1.47:1. In comparison, "brogrammermaid" (although an illegal generalized portmanteau) has a compression ratio of  ${}^{24}/_{14} = 1.71:1$ . So it is fair to say that we are in the ballpark of a "solid portmanteau." Of course, the gold standard is a compression ratio of  $\infty : 1$ —for the case that we have the word portmanteau, a totally overlapping portmanteau of portmanteau + portmanteau,<sup>6</sup> iterated infinitely.

<sup>&</sup>lt;sup>5</sup>There are some rubs: TSP requires that nodes only be visited once but a portmantout can use words multiple times. I believe that the multi-visit generalization of TSP is also NP-hard. The portmantout solution also requires visiting every edge, but we can relax this by concatenating all edge words e into a new mega-long word like  $e_0 z e_1 z \ldots e_k$  where z is also a fresh symbol; since this word must appear and all edges are substrings of it, we now have no requirement that the rest of the solution (containing our TSP embedding) contains all edge words. This kind of trick also lets us set the start node for TSP.

<sup>&</sup>lt;sup>6</sup>Cara Gillotti, personal communication, 2015.

	a	b	с	$\mathbf{d}$	e	f	g	h	i	j	k	1	m
a	anna	arab	arc	add	ace	agof	aleg	ash	ansi	arconj	ark	ail	am
b	boa	bib	barc	bad	be	barf	bag	bach	bassi	baconj	back	bail	bum
с	cia	cab	calc	$\operatorname{cod}$	cue	calf	cog	cash	cacti	conj	calk	call	cum
d	dada	dab	doc	dad	die	dof	dig	dash	deli	deconj	dank	deal	dam
e	era	ebb	etc	end	eve	elf	egg	each	elhi	econj	elk	eel	elm
f	feta	fib	farc	fad	fee	fief	fag	fish	fbi	falconj	fink	fail	farm
$\mathbf{g}$	gaga	gab	getc	god	gage	gof	gag	gash	genii	garconj	gawk	gal	gem
$\mathbf{h}$	hula	hub	hetc	had	he	half	hag	hash	haji	hadj	hack	hail	ham
i	idea	iamb	isac	ibid	ice	if	ifag	inch	ifbi	iconj	ilk	ill	ibm
j	java	jab	jarc	jaded	joe	jiff	jig	josh	jinni	jehadj	jack	jail	jam
k	kaka	kerb	kepic	kid	kale	kerf	keg	kith	kepi	kashadj	kick	keel	kakam
1	lava	lab	letc	lad	lie	leaf	lag	lash	levi	loconj	lack	loll	loam
$\mathbf{m}$	mama	$\operatorname{mob}$	mac	mad	me	$\operatorname{miff}$	$\operatorname{meg}$	mach	magi	maconj	mack	mail	mom
$\mathbf{n}$	nasa	nab	narc	nod	name	nof	nag	nigh	nazi	narconj	nark	nil	nam
0	ova	orb	orc	odd	ode	of	orig	ooh	ofbi	oohadj	oak	oil	ovum
$\mathbf{p}$	pea	pub	proc	pad	pee	pelf	$\operatorname{peg}$	$\operatorname{path}$	padri	poconj	pack	pal	palm
$\mathbf{q}$	qiana	qaidab	quebec	qaid	quake	quaff	quahog	qoph	quasi	qophadj	quack	quail	quam
$\mathbf{r}$	raga	rib	rabic	rad	rue	ref	rag	rash	rani	reconj	rack	rail	ram
S	sea	sob	sac	sad	see	sof	sag	sash	ski	shadj	sack	sail	sam
t	tea	tub	talc	tad	tee	tof	tag	tach	taxi	taconj	tack	tail	tım
u	usa	upub	uric	used	use	utot	ufog	ugh	ugli	ughadj	umiak	ural	unum
v	via	verb	vetc	veld	vade	vetof	vying	vetch	verdi	vaticonj	vailk	vail	viam
w	wnoa	web	warc	wad	we	wali	wag	wasn	wadi	wasnadj	WOK	wall	warm
x	xenia	xmasob	xebec	xyloid	xylene	xmaself	xmasag	xmasn	xmaski	xebeconj	xmask	xylitol	xylem
У	ymca	yamob	yetc	yard	yaie	yarei	yang	yean	yeti	yeanadj	уак	yawı	yam
Z	zeta	zagab	ZIIIC	zena	zone	2001	zag	ZOOH	zum	zinconj	zooak	zear	ZOOIII
		~		-		~	1						
	n	0	p	q	r	S	t	u adiou	v	W	X	y	Z
a h	n an ban	<b>o</b> ago bio	<b>p</b> amp bop	<b>q</b> airaq bassiraq	r air bar	s as bus	t at bat	<b>u</b> adieu beau	<b>v</b> atv batv	w anew bow	<b>x</b> apex box	<b>y</b> any by	<b>z</b> abuzz
a b	n an ban can	o ago bio ciao	<b>p</b> amp bop	<b>q</b> airaq bassiraq colloq	<b>r</b> air bar car	s as bus cabs	t at bat cat	<b>u</b> adieu beau chou	<b>v</b> atv batv	<b>w</b> anew bow	x apex box caly	<b>y</b> any by	<b>z</b> abuzz buzz chez
a b c d	n an ban can dan	o ago bio ciao do	<b>p</b> amp bop cap dip	<b>q</b> airaq bassiraq colloq deairaq	<b>r</b> air bar car dor	<b>s</b> as bus cabs dis	t at bat cat dot	<b>u</b> adieu beau chou dayou	<b>v</b> atv batv catv dotv	<b>w</b> anew bow cow dew	<b>x</b> apex box calx deux	y any by coy day	<b>z</b> abuzz buzz chez dovez
a b c d e	n an ban can dan eon	o ago bio ciao do ego	<b>p</b> amp bop cap dip emup	<b>q</b> airaq bassiraq colloq deairaq emiraq	r air bar car dor ear	s as bus cabs dis ears	t at bat cat dot eat	<b>u</b> adieu beau chou dayou emu	<b>v</b> atv batv catv dotv eatv	<b>w</b> anew bow cow dew eraw	x apex box calx deux eaux	<b>y</b> any by coy day easy	<b>z</b> abuzz buzz chez doyez elfez
a b c d e f	n an ban can dan eon fan	o ago bio ciao do ego faro	<b>p</b> amp bop cap dip emup fop	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq	r air bar car dor ear far	s as bus cabs dis ears fads	t at bat cat dot eat fat	<b>u</b> adieu beau chou dayou emu flu	<b>v</b> atv batv catv dotv eatv fatv	w anew bow cow dew eraw few	x apex box calx deux eaux fax	<b>y</b> any by coy day easy fey	<b>z</b> abuzz buzz chez doyez elfez fez
a b c d e f	n an ban can dan eon fan gin	o ago bio ciao do ego faro go	<b>p</b> amp bop cap dip emup fop gap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq	r air bar car dor ear far gor	s as bus cabs dis ears fads gas	t at bat cat dot eat fat get	<b>u</b> adieu beau chou dayou emu flu gnu	v atv batv catv dotv eatv fatv getv	w anew bow cow dew eraw few glow	x apex box calx deux eaux fax galax	y any by coy day easy fey gay	z abuzz buzz chez doyez elfez fez grosz
a b c d e f g h	n an ban can dan eon fan gin hen	o ago bio ciao do ego faro go halo	p amp bop cap dip emup fop gap hip	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq	r air bar car dor ear far gor her	s as bus cabs dis ears fads gas has	t at bat cat dot eat fat get hat	u adieu beau chou dayou emu flu gnu hemu	v atv batv catv dotv eatv fatv getv hatv	w anew bow cow dew eraw few glow how	x apex box calx deux eaux fax galax hex	y any by coy day easy fey gay hay	z abuzz buzz chez doyez elfez fez grosz hertz
a b c d e f g h i	n an ban can dan eon fan gin hen in	o ago bio ciao do ego faro go halo ino	p amp bop cap dip emup fop gap hip imp	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq	r air bar car dor ear far gor her intr	s as bus cabs dis ears fads gas has is	t at bat cat dot eat fat get hat it	u adieu beau chou dayou emu flu gnu hemu iflu	v atv batv catv dotv eatv fatv getv hatv itv	w anew bow cow dew eraw few glow how ifew	x apex box calx deux eaux fax galax hex ibex	y any by coy day easy fey gay hay icy	z abuzz buzz chez doyez elfez fez grosz hertz ifez
a b c d e f g h i j	n an ban can dan eon fan gin hen in jean	o ago bio ciao do ego faro go halo ino jato	<b>p</b> amp bop cap dip emup fop gap hip imp jeep	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq	r air bar car dor ear far gor her intr jar	s as bus cabs dis ears fads gas has is jabs	t at bat cat dot eat fat get hat it jet	u adieu beau chou dayou emu flu gnu hemu iflu juju	v atv batv catv dotv eatv fatv getv hatv itv jetv	w anew bow cow dew eraw few glow how ifew jaw	x apex box calx deux eaux fax galax hex ibex jeux	y any by coy day easy fey gay hay icy jay	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz
a b c d e f g h i j k	n an ban can dan eon fan gin hen in jean ken	o ago bio ciao do ego faro go halo ino jato kayo	p amp bop cap dip emup fop gap hip imp jeep keep	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq	r air bar car dor ear far gor her intr jar kafir	s as bus cabs dis ears fads gas has is jabs kays	t at bat cat dot eat fat get hat it jet kit	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev	w anew bow cow dew eraw few glow how ifew jaw knew	x apex box calx deux eaux fax galax hex ibex jeux knox	y any by coy day easy fey gay hay icy jay key	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz
a b c d e f g h i j k l	n an ban can dan eon fan gin hen in jean ken lain	o ago bio ciao do ego faro go halo ino jato kayo leo	p amp bop cap dip emup fop gap hip imp jeep keep lap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq	r air bar car dor ear far gor her intr jar kafir lair	s as bus cabs dis ears fads gas has is jabs kays labs	t at bat cat dot eat fat get hat it jet kit let	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv	w anew bow cow dew eraw few glow how ifew jaw knew law	x apex box calx deux eaux fax galax hex ibex jeux knox lax	y any by coy day easy fey gay hay icy jay key lay	z abuzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz
a b c d e f g h i j k l m	n an ban can dan eon fan gin hen in jean ken lain man	o ago bio ciao do ego faro go halo ino jato kayo leo moo	p amp bop cap dip emup fop gap hip imp jeep keep lap map	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq	r air bar car dor ear far gor her intr jar kafir lair moor	s as bus cabs dis ears fads gas has is jabs kays labs macs	t at bat cat dot eat fat get hat it jet kit let mat	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv	w anew bow cow dew eraw few glow how ifew jaw knew law	x apex box calx deux eaux fax galax hex jeux knox lax max	y any by coy day easy fey gay hay icy jay key lay my	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez
a b c d e f g h i j k l m n	n an ban can dan eon fan gin hen in jean ken lain man non	o ago bio ciao do ego faro go halo ino jato kayo leo moo no	p amp bop cap dip emup fop gap hip imp jeep keep lap map nap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq	r air bar car dor ear far gor her intr jar kafir lair moor nor	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs	t at bat cat dot eat fat get hat it jet kit let mat net	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new	x apex box calx deux eaux fax galax hex ibex jeux knox lax max nix	y any by coy day easy fey gay hay icy jay key lay my nay	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz
a b c d e f g h i j k l m n o	n an ban can dan eon fan gin hen in jean ken lain man non on	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono	p amp bop cap dip emup fop gap hip imp jeep keep lap map nap ofop	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs	t at bat cat dot eat fat get hat it jet kit let mat net oat	u adieu beau chou dayou emu flu gnu hemu juju kudu lieu menu nehru oflu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew	x apex box calx deux eaux fax galax hex ibex jeux knox lax max nix onyx	y any by coy day easy fey gay hay icy jay key lay my nay obey	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez
a b c d e f g h i j k l m n o p	n an ban can dan eon fan gin hen in jean ken lain man non on pan	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono paso	p amp bop cap dip emup fop gap hip imp jeep keep lap map nap ofop pep	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus	t at bat cat dot eat fat get hat it jet kit let mat net oat pat	u adieu beau chou dayou emu flu gnu hemu juju kudu lieu menu nehru oflu peru	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw	x apex box calx deux eaux fax galax hex ibex jeux knox lax max nix onyx pox	y any by coy day easy fey gay hay icy jay key lay my nay obey pay	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz
a b c d e f g h i j k l m n o p q	n an ban can dan eon fan gin hen in jean ken lain man non on pan quean	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono paso quito	p amp bop cap dip emup fop gap hip imp jeep keep lap map ofop pep quip	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq quasiraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par qatar	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus ques	t at bat cat dot eat fat get hat it jet kit let mat net oat pat quit	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru oflu peru quipu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv quitv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw qaidew	x apex box calx deux eaux fax galax hex ibex jeux knox lax max nix onyx pox qophex	y any by coy day easy fey gay hay icy jay key lay my nay obey pay quaky	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz quiz
a b c d e f g h i j k l m n o p q r	n an ban can dan eon fan gin hen in jean ken lain man non on pan quean ran	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono paso quito redo	p amp bop cap dip emup fop gap hip imp jeep keep lap map nap ofop pep quip rap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq quasiraq raniraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par qatar rear	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus ques rads	t at bat cat dot eat fat get hat it jet kit let mat net oat pat quit rat	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru oflu peru quipu ragnu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv quitv ratv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw qaidew raw	x apex box calx deux eaux fax galax hex jeux knox lax max nix onyx pox qophex roux	y any by coy day easy fey gay hay icy jay key lay my nay obey pay quaky ray	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz quiz razz
a b c d e f g h i j k l m n o p q r s	n an ban can dan eon fan gin hen in jean ken lain man non on pan quean ran sin	o ago bio ciao do ego faro go halo ino jato kayo leo moo no paso quito redo so	pampbopcapdipemupfopgaphipimpjeepkeeplapmapofoppepquiprapsap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq quasiraq raniraq siraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par qatar rear sir	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus ques rads sos	t at bat cat dot eat fat get hat it jet kit let mat net oat pat quit rat sat	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru oflu peru quipu ragnu situ	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv quitv ratv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw qaidew raw saw	x apex deux deux fax galax hex jeux knox lax max nix onyx pox qophex roux sax	y any by coy day easy fey gay hay icy jay key lay my nay obey pay quaky ray say	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz quiz razz sitz
a b c d e f g h i j k l m n o p q r s t	n an ban can dan eon fan gin hen in jean ken lain man non on pan quean ran sin tan	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono paso quito redo so to	pampbopcapdipemupfopgaphipimpjeepkeeplapmapofoppepquiprapsaptap	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq quasiraq raniraq siraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par qatar rear sir tar	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus ques rads sos tis	t at bat cat dot eat fat get hat it jet kit let mat net oat pat quit rat sat tit	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru oflu peru quipu ragnu situ tabu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv quitv ratv shiv	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw qaidew raw saw tow	x apex calx deux eaux fax galax hex jeux knox lax max nix onyx pox qophex roux sax tax	y any by coy day easy fey gay hay icy jay key lay my nay obey pay quaky ray say thy	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz quiz razz sitz tviz
a b c d e f g h i j k l m n o p q r s t u	n an ban can dan eon fan gin hen in jean ken lain man non on pan quean ran sin tan urn	o ago bio ciao do ego faro go halo ino jato kayo leo moo no ono paso quito redo so to ufo	p amp bop cap dip emup fop gap hip imp jeep keep lap map nap ofop pep quip rap sap tap up	<b>q</b> airaq bassiraq colloq deairaq emiraq firaq geniiraq hairaq iraq jinniraq kafiraq liraq magiraq noiraq obeliraq pairaq quasiraq siraq tapiraq ugliraq	r air bar car dor ear far gor her intr jar kafir lair moor nor or par qatar rear sir tar user	s as bus cabs dis ears fads gas has is jabs kays labs macs nabs oafs pus ques rads sos tis us	t at bat cat dot eat fat get hat it jet kit let mat net oat pat quit rat sat tit unit	u adieu beau chou dayou emu flu gnu hemu iflu juju kudu lieu menu nehru oflu peru quipu ragnu situ tabu uperu	v atv batv catv dotv eatv fatv getv hatv itv jetv kiev letv mirv netv oatv patv quitv ratv shiv tv univ	w anew bow cow dew eraw few glow how ifew jaw knew law mow new odew paw qaidew raw saw tow upaw	x apex calx deux eaux fax galax hex jeux knox lax max nix onyx pox qophex roux sax tax unix	y any by coy day easy fey gay hay icy jay key lay my nay obey pay quaky ray say thy ugly	z abuzz buzz chez doyez elfez fez grosz hertz ifez jazz klutz leviz machez nertz oyez phiz quiz razz sitz tviz uphiz
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Figure 1: Minimal joining strings for every letter (rows) to every other letter (columns).

















